

6.6(b)

→ Based on LR Parsing for the following grammar show all steps for the stack, input and Action.

Ans. Given Grammar,

$$E \rightarrow E + T$$

$$E \rightarrow T$$

$$T \rightarrow T * F$$

$$T \rightarrow F$$

$$F \rightarrow (E)$$

$$F \rightarrow id$$

Q6.6) Based on LR Parsing, for the following grammar!
 show all steps for stack input and Action. [id+id*id]

step	stack	input	Action
1		id+id*id\$	shift id
2	id	+id*id\$	Reduce $F \rightarrow id$
3	F	+id*id\$	Reduce $T \rightarrow F$
4	T	+id*id\$	Reduce $E \rightarrow T$
5	E	+id*id\$	shift +
6	E+	id*id\$	shift id
7	E+id	*id\$	Reduce $F \rightarrow id$
8	E+F	*id\$	Reduce $T \rightarrow F$
9	E+T	*id\$	shift *
10	E+T*	id\$	shift id
11	E+T*id	\$	Reduce $F \rightarrow id$
12	E+T*F	\$	Reduce $T \rightarrow T*F$
13	E+T	\$	Reduce $E \rightarrow E+T$
14	E	\$	Accepted.

target: Rules starting reduce 400/1

6.1a Describe Algorithm for LR Parser.

Ans: Algorithm:

1. Initialize

stack $\leftarrow$ [$\$$] // $\$$ is the initial state

Input $\leftarrow$ w $\$$ // input string with end marker.

2. Repeat:

Let s be top state on the stack.

Let a be the current input symbol.

a) If $Action[s, a] = \text{shift } t$

— push symbol a and state t onto the stack

— Advance input to next symbol.

b) If $Action[s, a] = \text{reduce } A \rightarrow B$

— pop $|A|$ from stack (since both symbol & state)

— let s' be the new top state

— push A and $GOTO[s', \#]$ on the stack.

c) IF ACTION[s, a] = Accept;
 — parsing successful, return Accept

d) IF ACTION = error
 — report system error.

3. End of Algorithm.

⑦ b. given, $s \rightarrow (L)/a$
 $L \rightarrow L, s/s$

Step 1: Eliminate left recursion:

The grammar has left recursion in production for L. so the grammar becomes.

$L \rightarrow L, s/s$

so the grammar becomes.

Rewrite it, As

$s \rightarrow (L)/a$

$L \rightarrow SL'$

$L \rightarrow SL'$

$L' \rightarrow , SL' / \epsilon$

$L' \rightarrow , SL' / \epsilon$

Steps: Find First and Follow.

$$\text{FIRST}(S) = \langle (, a \rangle$$

$$\text{FIRST}(L) = \langle (, a \rangle$$

$$\text{FIRST}(L') = \langle ', \epsilon \rangle$$

$$\text{Follow}(S) = \langle \$, ' \rangle$$

$$\text{Follow}(L) = \langle ' \rangle$$

$$\text{Follow}(L') = \langle ' \rangle$$

Steps construct Predictive Parsing table:

Non-Terminal	(	a	'	,	\$
S	$S \rightarrow (L$	$S \rightarrow a$			
L	$L \rightarrow SL'$	$L \rightarrow SL'$			
L'			$L' \rightarrow ', SL'$	$L' \rightarrow \epsilon$	

8.9

Rule	First	Follow
$E \rightarrow TE_R$	$(, id$	$),$
$E_R \rightarrow +TE_R \epsilon$	$+, \epsilon$	$),$
$T \rightarrow FT_R$	$(, id$	$+,)$
$T_R \rightarrow *FT_R \epsilon$	$*, \epsilon$	$+,),$
$F \rightarrow (E) id$	$(, id$	$*, +,),$

9 #NFA to DFA: subset construction Method.

1. NFA $\rightarrow$ start $\rightarrow$ final (2, 4)

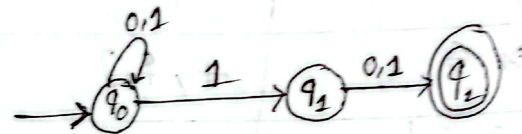
2. DFA $\rightarrow$ start $\rightarrow$ final (1, 4, 5)
Initial state same as NFA

6.4.a

→ write down the NFA of all binary strings in which second, last, bit is 1. convert the NFA into DFA.

Ans:

Accepted Language: 10, 11, 00010, 11110, ...



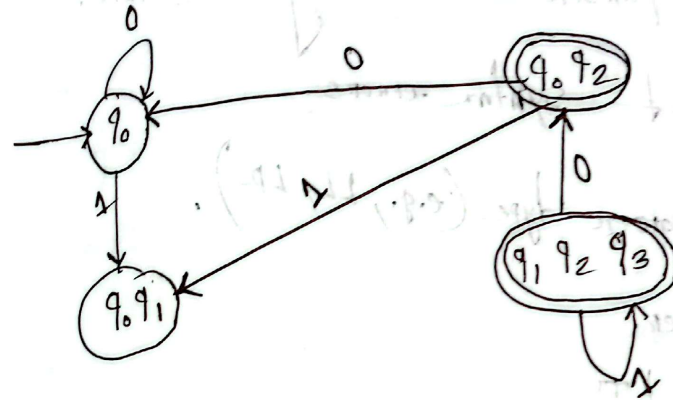
→ Create state transition table for NFA.

state	input	
	0	1
→ q ₀	q ₀	{q ₀ , q ₁ }
q ₁	q ₂	q ₂
*q ₂	∅	∅

→ Now convert this table for DFA.

state	0	1
→ q ₀	q ₀	[q ₀ , q ₁]
[q ₀ , q ₁]	[q ₀ , q ₂]	[q ₀ , q ₁ , q ₂]
*[q ₀ , q ₂]	[q ₀]	[q ₀ , q ₁]

state transition diagram!



5.a

Parser:

A Parser is a component of a compiler that takes input in form of a sequence of tokens (produced by the lexical Analyzer) and check it against the rules defined by the grammar. Its main task is to determine wheather the input syntactically correct and to build a parse tree or sytam tree that represents the structure of the input.

Role of a grammar in parse construction:

- Defines syntax rules of language
- Guides the parser in constructing parse tree.
- Helps detect syntax errors.
- Determine parser type (e.g., LL, LR).

Given grammar:

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid id$$

It has left recursive. Remove it, and then —

$$E \rightarrow TE'$$

$$E \rightarrow +TE' \mid \epsilon$$

$$T \rightarrow TF$$

$$T \rightarrow F$$

$$F \rightarrow (E) \mid id$$

Parse table with
LR(0) items

Q.1 Design a recursive descent parser for the grammar:

Ans: Given Grammar:

$E \rightarrow E + T \mid T$ [has left recursion]

$T \rightarrow T * F \mid F$ [Also has "]

$F \rightarrow (E) \mid id.$

Step 1: For recursive descent, the grammar must not be left recursive. so we have to remove eliminate all " "

- For E:

$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \epsilon$

- For T:

$T \rightarrow T * F \mid F$

- $T \rightarrow FT^*$

- $T' \rightarrow *FT' \mid \epsilon$

Transformed Grammar:

$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \epsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \epsilon$

$F \rightarrow (E) \mid id.$

Steps: Pseudocode for Recursive Descent Parser.

```
void E() {  
    T();  
    E-Prime();  
}
```

```
void E-Prime() {  
    if (lookahead == '+') {  
        match('+');  
        T();  
        E-Prime();  
    }  
    else epsilon  
}
```

```
void T-Prime() {  
    if (lookahead == '*') {  
        match('*');  
        F();  
        T-Prime();  
    }  
    else epsilon  
}
```

```

void F() {
    if (lookahead == '(') {
        match('(');
        E();
        match('(');
    }
    else if (lookahead == 'id') {
        match('id');
    }
    else return();
}

```

Q. Given grammar:

$S \rightarrow aABe$
 $A \rightarrow Abe \mid b$ (has left recursion, we have to remove it)
 $B \rightarrow d$

↓ Transform grammar:

$S \rightarrow aAB'e$
 $A \rightarrow bA'$
 $A' \rightarrow beA' \mid \epsilon$
 $B \rightarrow d$

Non-Terminal	First	Follow
S	{a}	{\$, }
A	{b}	{d}
A'	{b, ϵ }	{d}
B	{d}	{ ϵ }

Q. What is Recursive Descent parsing? List the problem faced in designing such parser.

Ans: It is a top down parsing method where each non-terminal in the grammar is implemented as a recursive function. These functions process the input and check if it matches the grammar.

Problem in designing Recursive Descent parser:

1. Left Recursion: Cause infinite recursion. must be removed.

2. Backtracking: Required when alternatives begin with some symbol, making parsing inefficient.

3. Ambiguity: Difficult to handle as multiple parse trees are possible.

4. Predictive Limitations: Works only for grammar suitable for Predictive Parsing ($LL(1)$)

5. Error handling: Manual handling is needed for detecting and recovering from errors.

3.4

Leftmost Derivation

→ Always replaces the leftmost non-terminal first

→ Derivation proceeds from left to right

→ used in LL parsers
(top-down parsing)

Ex. given Grammar.

$S \rightarrow AB$

$A \rightarrow a$

$B \rightarrow b$

⇒ $\boxed{ab}$
 $S \rightarrow AB$

$\rightarrow aB$

$\rightarrow ab.$

Rightmost Derivation

→ Always replaces rightmost non-terminal first.

→ Derivation proceeds from right to left.

→ used in LR parsers
(bottom-up parsing)

Ex.

$S \rightarrow AB$

$A \rightarrow a$

$B \rightarrow b$

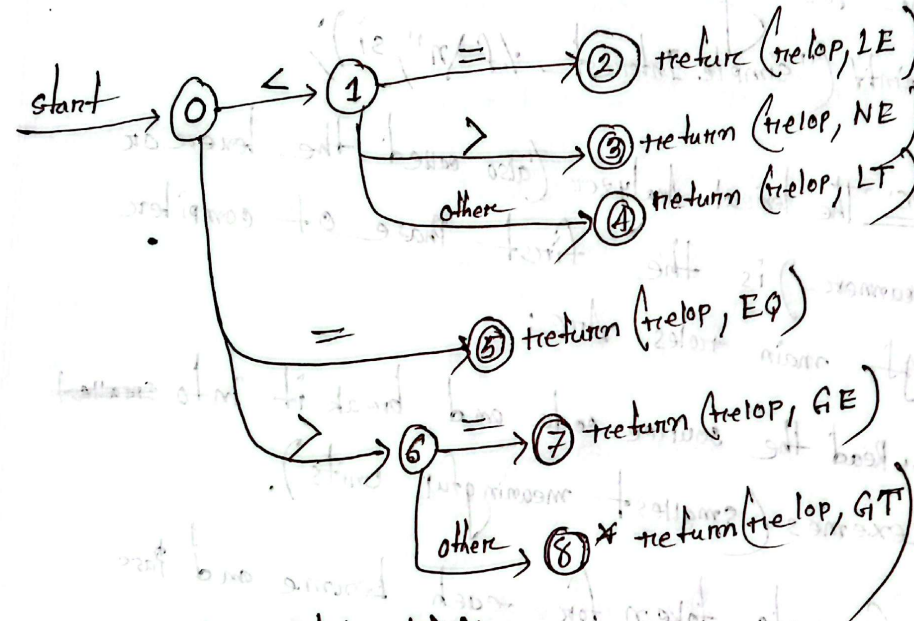
string: ab

$S \rightarrow AB$

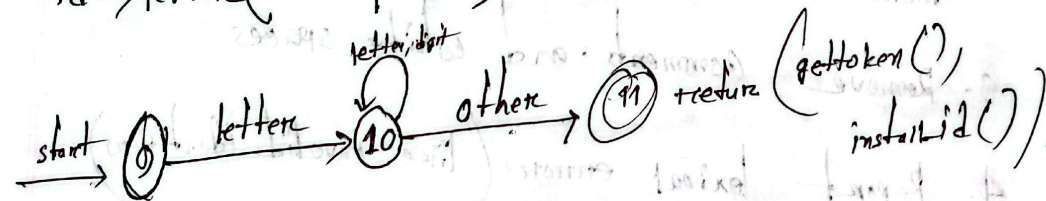
$\rightarrow Ab$

$\rightarrow ab.$

© Draw the transition diagram for the regular definition
 $\text{relop}() \quad < | < = | > | > = | >$



$\text{id} \rightarrow \text{letter}(\text{letter} | \text{digit})^*$



2. a) State the role of the lexical analyzer. Identify the lexemes and their corresponding tokens in the following statement:

```
printf("Simple Interest = %f\n", si);
```

Ans: The lexical analyzer (also called the lexer or scanner) is the first phase of compiler. Its main roles are:

1. Read the source code and break it into ~~statements~~ Lexemes (smallest meaningful units).
2. Generate token for each Lexeme and pass them into parser.
3. Remove comments and white spaces.
4. Report lexical errors (like invalid identifiers).

Lexeme	Token
Print	Identifier
(	LEFT_PAREN
"Simple integer rate"	STRING_LITERAL
,	COMMA
1	IDENTIFIER
si	IDENTIFIER
)	Right_Paren
;	SEMICOLON

(b) Discuss various Phases of Compiler and trace the Program segment $a = b * c * 50$ for all Phase.

Ans A compiler translates source code into machine code in multiple well-defined Phases. ~~Let~~ Let's discuss the Phases and trace the segment;
 ~~$a = b * c * 50$~~ $a = b + c * 50$.

1. Lexical Analysis:

→ Breaks the input into tokens

→ Lexemes & tokens:

Lexeme	Token
--------	-------

a

IDENTIFIER

=

ASSIGN-OP

b

IDENTIFIER

+

plus-OP

c

Identifier

*

Multi-OP

50

Number

;

SEMICOLON

2. Syntax Analysis: Builds a Parse tree based on grammar rules.

assignment $\rightarrow$ ID = expression

expression $\rightarrow$ ID + term

term $\rightarrow$ ID * Number

3. Semantic Analysis: Checks meaningful use of variable and operation

→ A variable declared.

→ A type compatible (e.g., 50 is valid for int/float).

4. Intermediate code generation: Converts code into three-address code

$$t_1 = c * 50$$

$$t_2 = b + t_1$$

$$a = t_2$$

5. Code optimization: Improve Performance without changing behaviour

→ if c is constant, $c * 50$ can be precalculated.

→ Reuse expression if possible.

6. Target code generation: Translates IR to Assembly code

MOV R1, C

MUL R1, 50

MOV R2, b

ADD R2, R1

MOV a, R2.

7. Code Linking & Link Assembly

Final Phase: resolve Address, links, libraries and create executable code.

$a < b$: shift
 $a > b$: reduce
 $a = b$: match Parenthesis

③ Using Operator Precedence relations, parse the string
 $id + (id * id)$

→ Define A Grammar:

$$E \rightarrow E + E \mid E * E \mid (E) \mid id.$$

$id \rightarrow$ any character
 $\$ \rightarrow$ end of string

→ Operator Precedence Table:

	id	+	*	\$
id	=	>	>	>
+	<	>	<	>
*	<	>	>	>
\$	<	<	<	=

Left side

* Terminal 0: 11/24
compare 0: 11/24.

stack	Input	Action.
\$	id + id * id \$	shift
\$id	+ id * id \$	id > +; reduce
\$E	+ id * id \$	\$ < +; shift
\$E+	id * id \$	+ < id; shift
\$E+id	* id \$	id > *; reduce
\$E+E	* id \$	\$ < *; shift
\$E+E*	id \$	* < id; shift
\$E+E*id	\$	id > \$; reduce
\$E+E*E	\$	* > \$ reduce
\$E+E	\$	+ > \$ reduce
\$E	\$	Accepted

1.2 Compiler: A Compiler is a Program that translates source code written in High Level Language into machine code or intermediate code.

Analysis & synthesis Model of a compiler:

(Front-end) Analysis Phase: Breaks source code into parts and build intermediate representation.

Phases:

1. Lexical Analysis: Converts input into tokens
2. Syntax Analysis: Build parse tree
3. Semantic Analysis: checks meaning and type.
4. Intermediate code generation: Produce it.

Synthesis phase (Back-end): Converts ~~to~~ intermediate representation to target code.

Phases:

1. Code optimization: Improve code efficiency.
2. Code generation: Generates machine code
3. Assembly and Linking: Combine all and produce executable.

⑥ given, $x = y * z + y * (-z)$

generate Three-Address code:

$$t_1 = y * z$$

$$t_2 = -z$$

$$t_3 = y * t_2$$

$$t_4 = t_1 + t_3$$

$$x = t_4$$

Index	Operator	Argument 1	Argument 2
0	*	y	z
1	uminus	z	
2	*	y	(1)
3	+	(0)	(2)
4	=	x	(3)

② Code optimization: is the process of improving the intermediate code to make program run faster, use less memory without changing its behaviour.

→ Types of optimization.

1. Machine-independent optimization: Applied before knowing the target machine.

Ex: $x = 2 + 3 \rightarrow x = 5$.
→ constant folding

→ Dead code elimination

→ Expression elimination

2. Machine Dependent Optimization:

- Applied after selecting the target machine
- Tailors code to specific Architecture (cpu, registers, instruction sets).

Example:

- Instruction scheduling
- Register Allocation
- Peephole optimization.

4d) Differentiate Tokens, Patterns, Lexeme:

Token: A category/class of lexical units (e.g., ID, Number)

Lexeme: Actual string of characters in the source code. (e.g., x, 123, if)

Pattern: Rule/regular expression that describes the structure of lexemes for a token.

Example: In the statement:

int x = 10;

Lexeme: int, x, =, 10;

Token: keyword, identifier, number, ~~number~~ identifier.

Pattern: Identifier $\rightarrow$ letter (letter | digit)*

Number $\rightarrow$ digit+.

6.2 LL(1) Grammar: An LL(1) grammar is type of context-free grammar that can be parsed by a top-down parser

using:

L: Left to right scanning of the input

L: Leftmost derivation

1: using one lookahead symbol (token) to make parsing decisions.

Given Grammar:

$$S \rightarrow iEs \mid iEs_s/a$$

$$E \rightarrow b$$

Both 1st & 2nd production of S start with iEs .

→ Left factoring of the grammar:

$$S \rightarrow iEs s'$$

$$s' \rightarrow \epsilon / es$$

$$s \rightarrow a$$

$$E \rightarrow b.$$

	First	Follow
ϵ		
s		
s'		

	First	Follow
S	{i, a}	{\$, e}
S'	{e, ε}	{\$, e}
E	{b}	{+}

Parsing Table:

Non terminal	i	a	b	e	+	\$
S	$S \rightarrow i E t S S'$	$S \rightarrow a$				
S'				$S' \rightarrow e$ $S' \rightarrow \epsilon$		
E			$E \rightarrow b$			

This grammar is not LL(1) because the Predictive Parse table contains multiple entries in the same cell (S', e) causing a First/Follow conflict.

In LL(1) grammar, each must have at most one production, which is not satisfied here.

$$E \rightarrow TE'$$

$$E' \rightarrow +TE'$$

$$E' \rightarrow \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT'$$

$$T' \rightarrow \epsilon$$

$$F \rightarrow (E)$$

$$F \rightarrow id$$

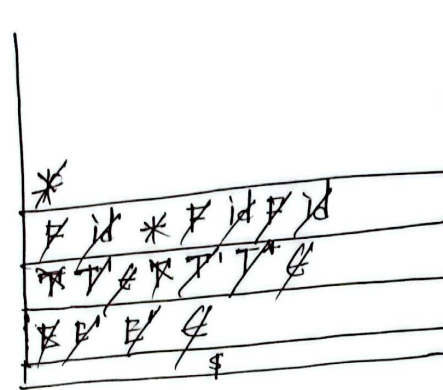
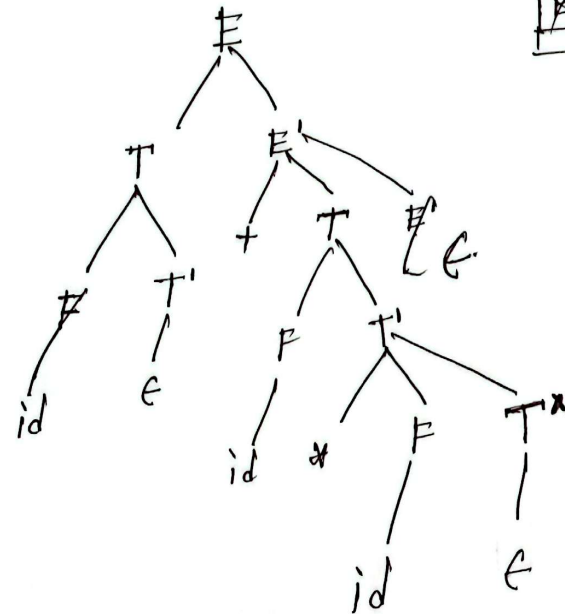
Find $F(E)$:-

5.4b

First	Follow	Non-terminal	+	*	(	)	id	\$
(, id	\$,)	E			$E \rightarrow TE'$		$E \rightarrow TE'$	
+ ϵ	\$,)	E'	$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$		$E' \rightarrow \epsilon$
(, id	+, \$,)	T			$T \rightarrow FT'$		$T \rightarrow FT'$	
* ϵ	+, \$,)	T'	$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$		$T' \rightarrow \epsilon$
(, id,	*, +, \$,)	F			$F \rightarrow (E)$		$F \rightarrow id$	

ning: id + id * id \$
 x x x x x

Parse Tree:



stack