

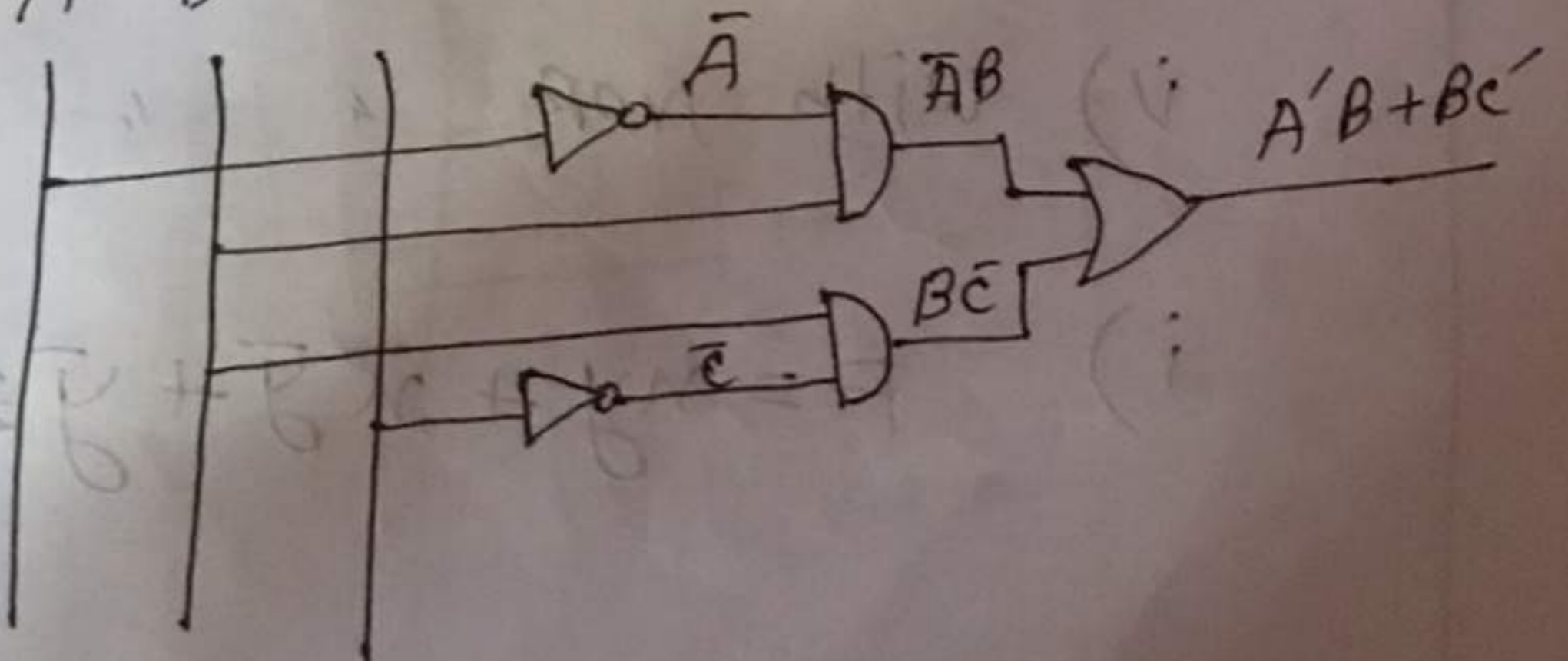
① Mention the duality principle?

The principle of duality is a kind of pervasive property of algebraic structure in which two principles or concepts are interchangeable only if all outcomes held true in one formulation are also held true in another. This concept is also referred to as "dual formulation".

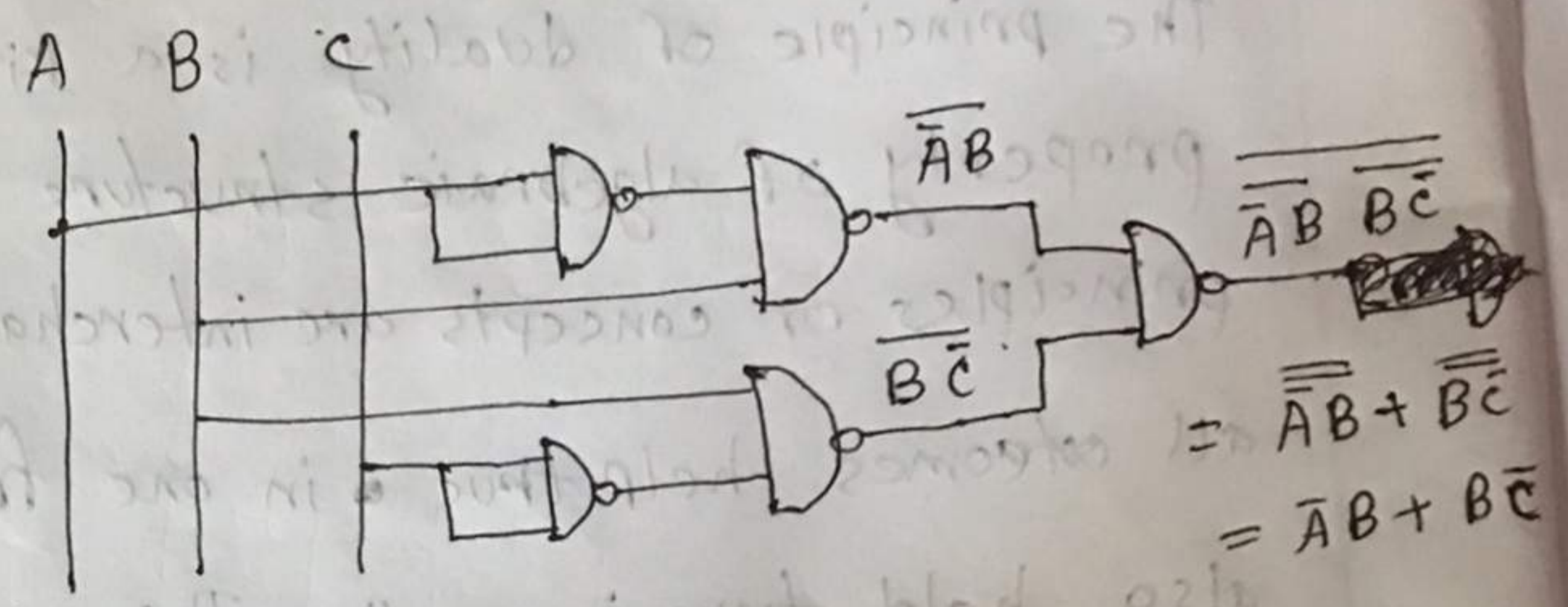
② Implement the function using NAND gate?

$$F = A'B + BC'$$

Logic gate:



### Implementation by NAND gate:

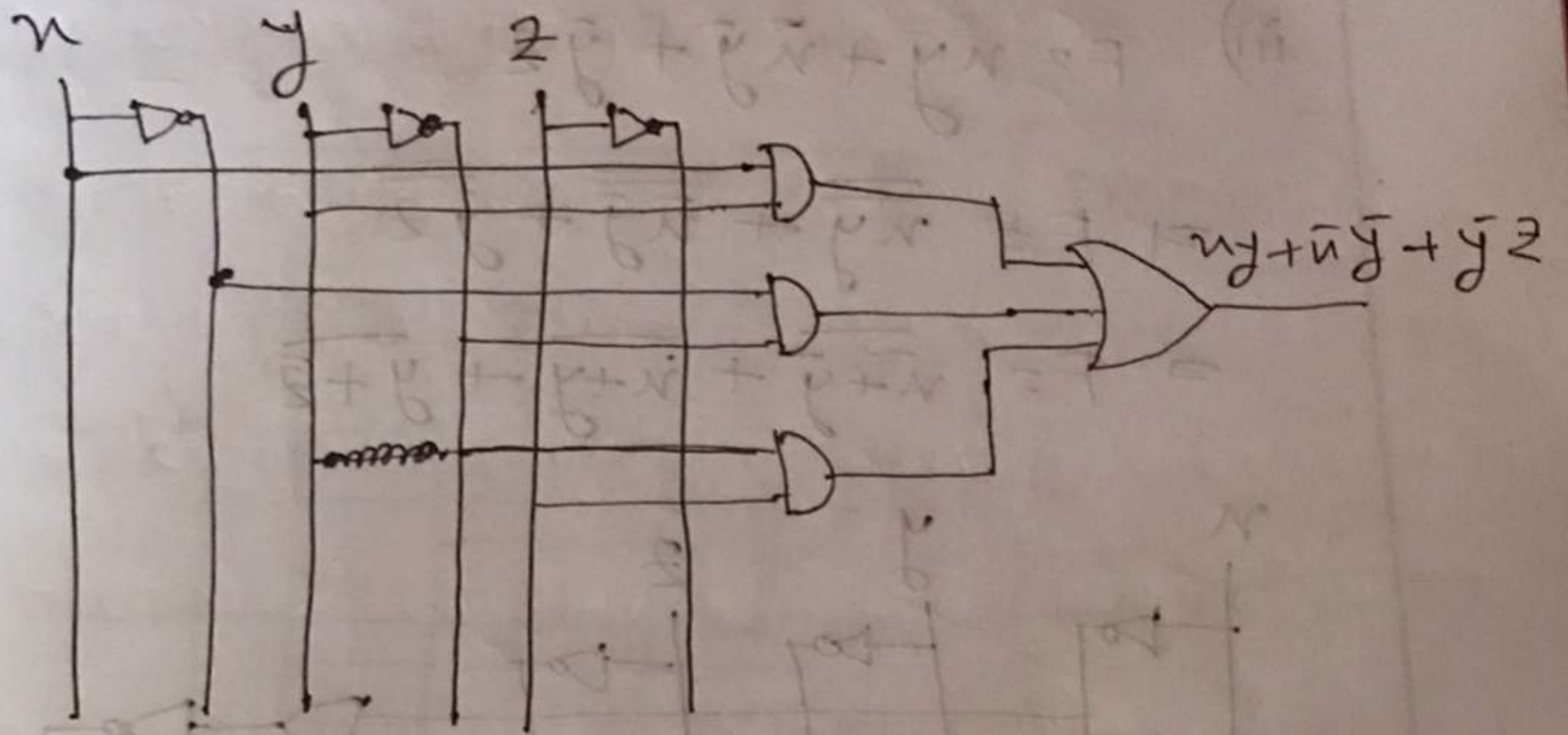


③ Implementation the Boolean function?

$$F = xy + x'y' + y'z$$

- i) with AND, OR, and Inverter gate
- ii) with AND and Inverters gate
- iii) with OR and " "
- iv) with NAND " " "
- v) with NOR " " "

i)  $F = xy + \overline{x}\overline{y} + y'z$

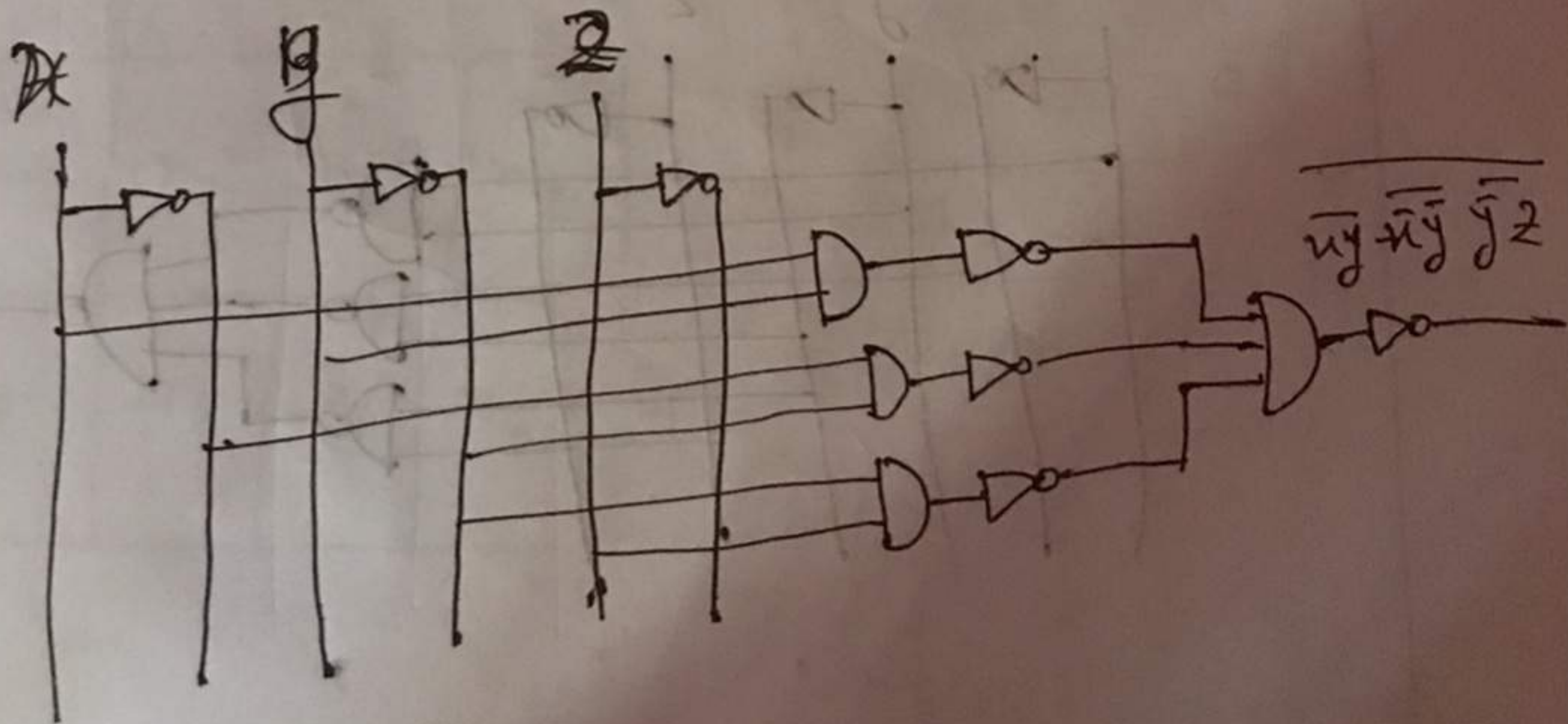


ii)  $F = xy + \bar{x}\bar{y} + yz$

$\Rightarrow F = \overline{xy + \bar{x}\bar{y} + yz}$

$\Rightarrow F = \overline{\overline{xy} \cdot \overline{\bar{x}\bar{y}} \cdot \overline{yz}}$

~~see the~~



~~$B + \bar{B}\bar{C}$~~   
 ~~$B + \bar{B}\bar{C}$~~   
 ~~$B + \bar{B}\bar{C}$~~

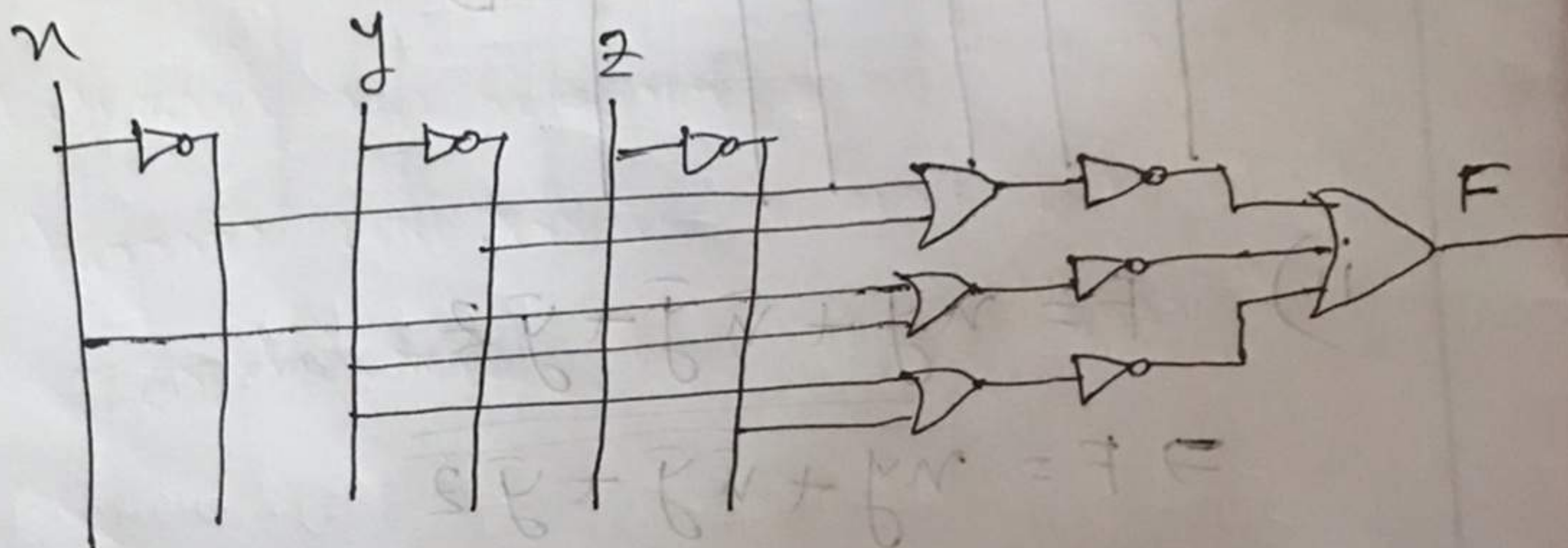
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$$\text{iii) } F = xy + \bar{x}\bar{y} + \bar{y}z$$

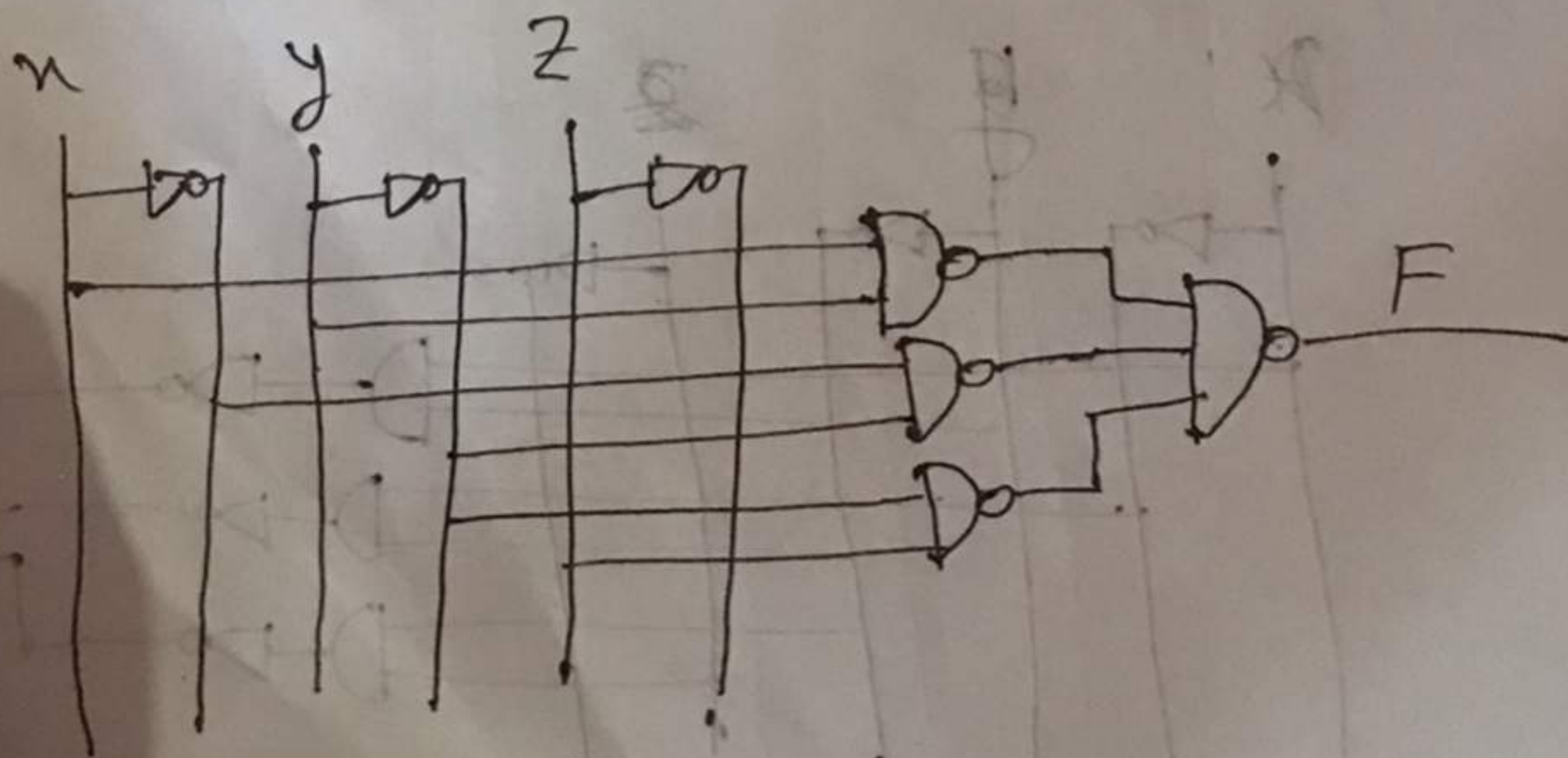
$$\Rightarrow F = \overline{\overline{xy}} + \overline{\overline{\bar{x}\bar{y}}} + \overline{\overline{\bar{y}z}}$$

$$\Rightarrow F = \overline{\bar{x} + \bar{y}} + \overline{x + y} + \overline{y + \bar{z}}$$



$$\text{iv) } F = xy + \bar{x}\bar{y} + \bar{y}z \quad \left[ \text{From (ii)} \right]$$

$$\Rightarrow F = \overline{\overline{xy}} \overline{\overline{\bar{x}\bar{y}}} \overline{\overline{\bar{y}z}}$$

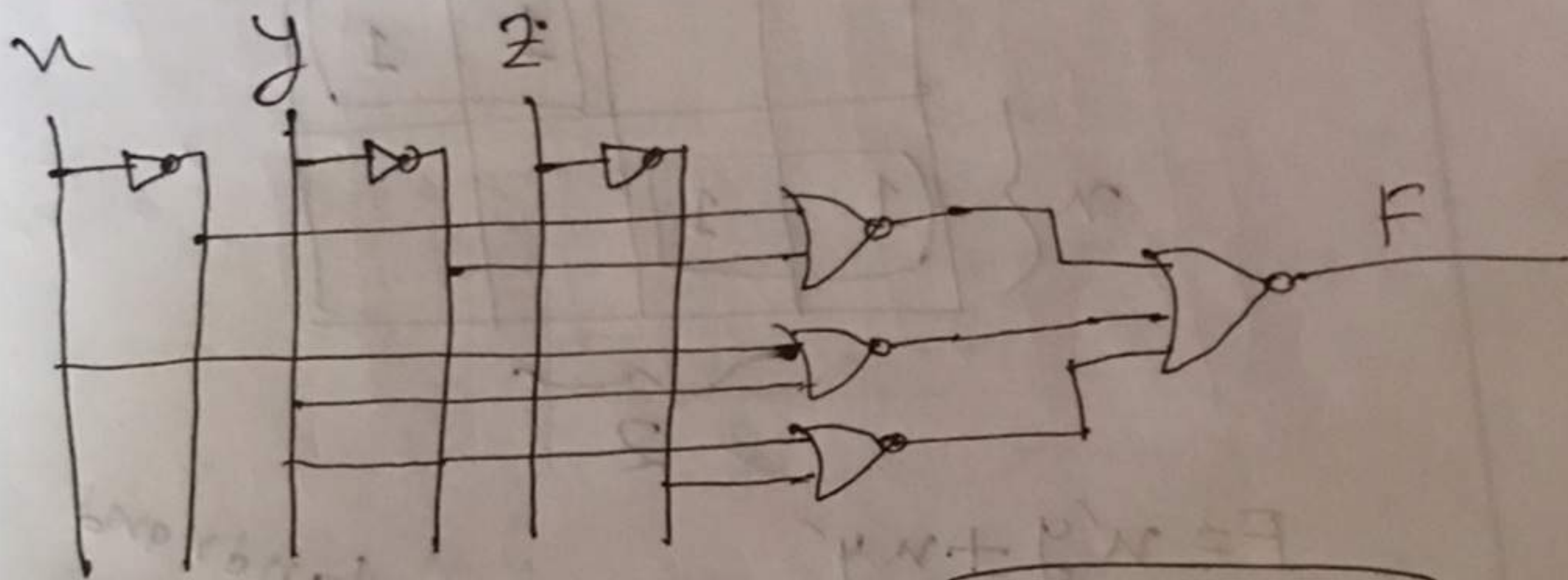


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④  $F = xy + \bar{x}y + yz$

$\Rightarrow F = \overline{x+y} + \overline{x+y} + \overline{y+z}$  (from iii)

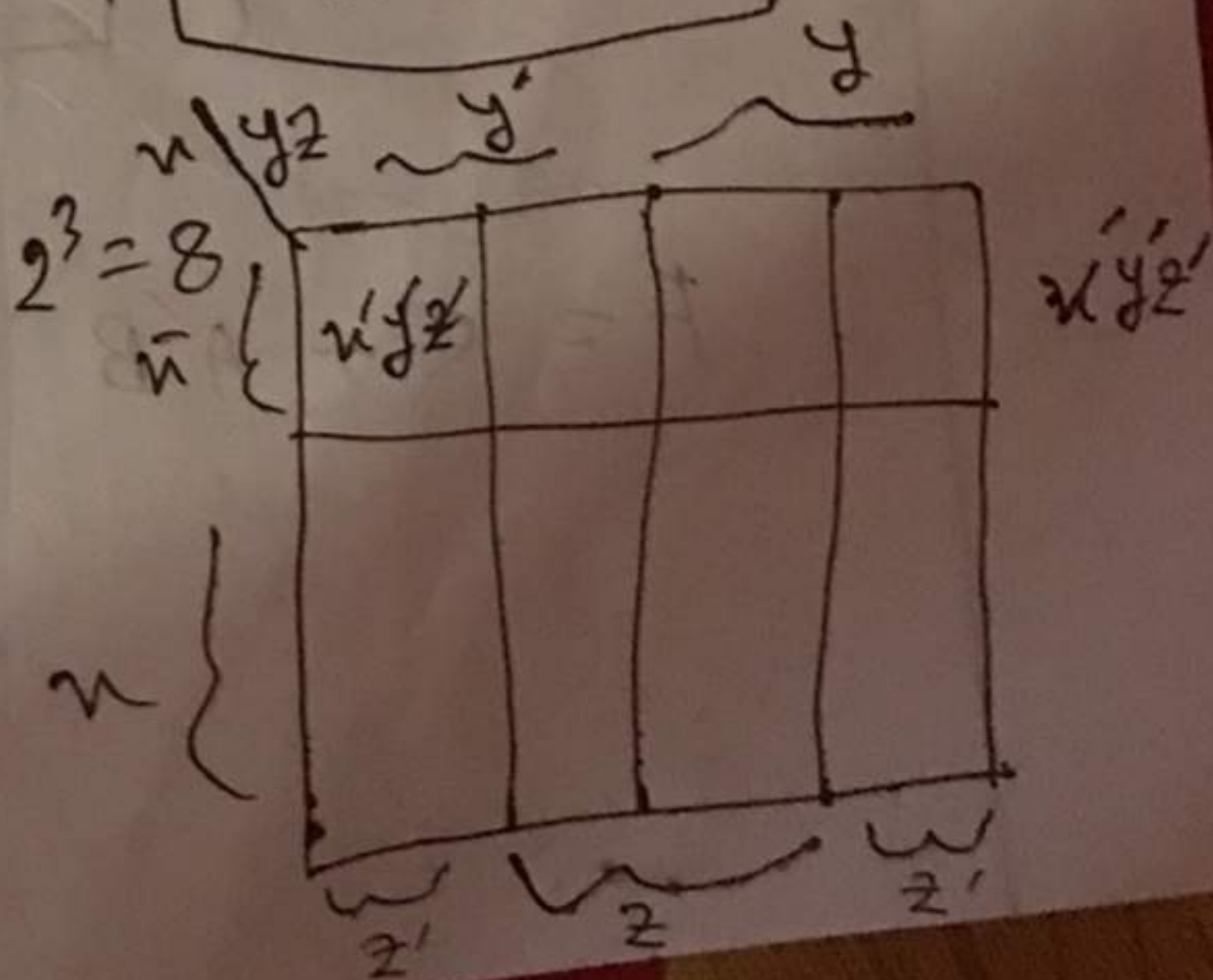
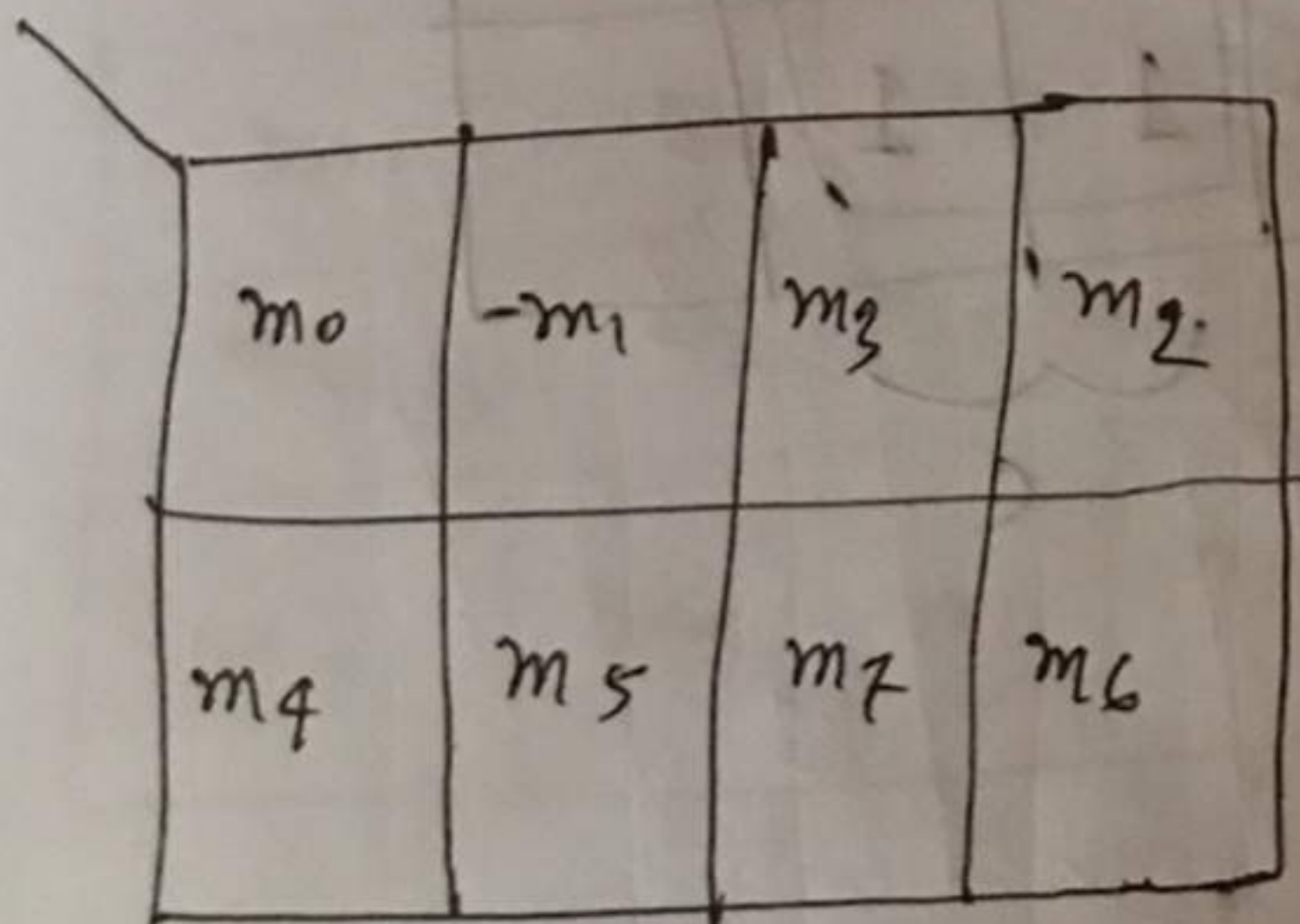


K-map

variable = 3

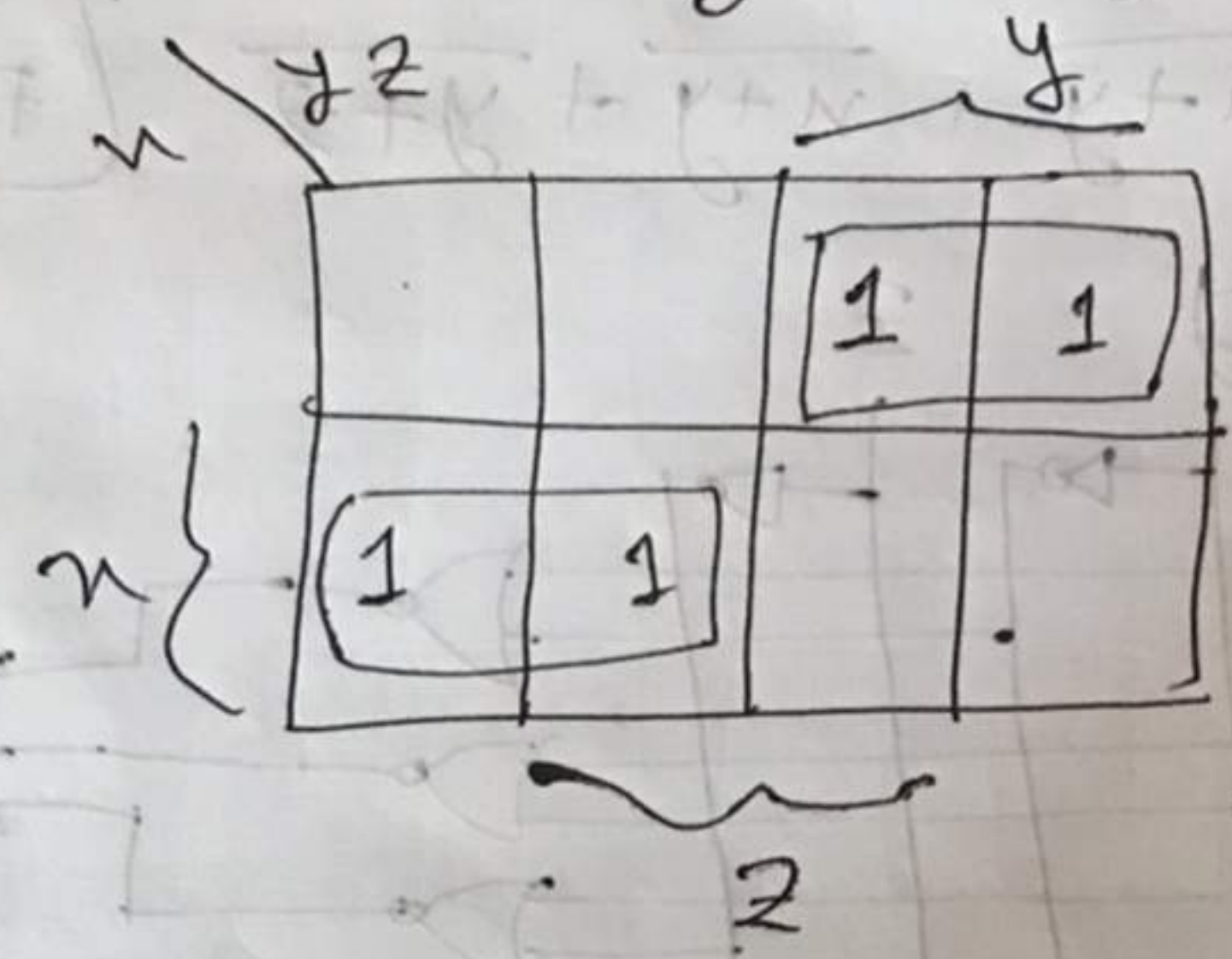
Note:

- $x+0 = x$
- $x+1 = 1$
- $x+x = x$
- $x+\bar{x} = 1$
- $x \cdot 0 = 0$
- $x \cdot 1 = x$
- $x \cdot x = x$
- $x \cdot \bar{x} = 0$



Standard form

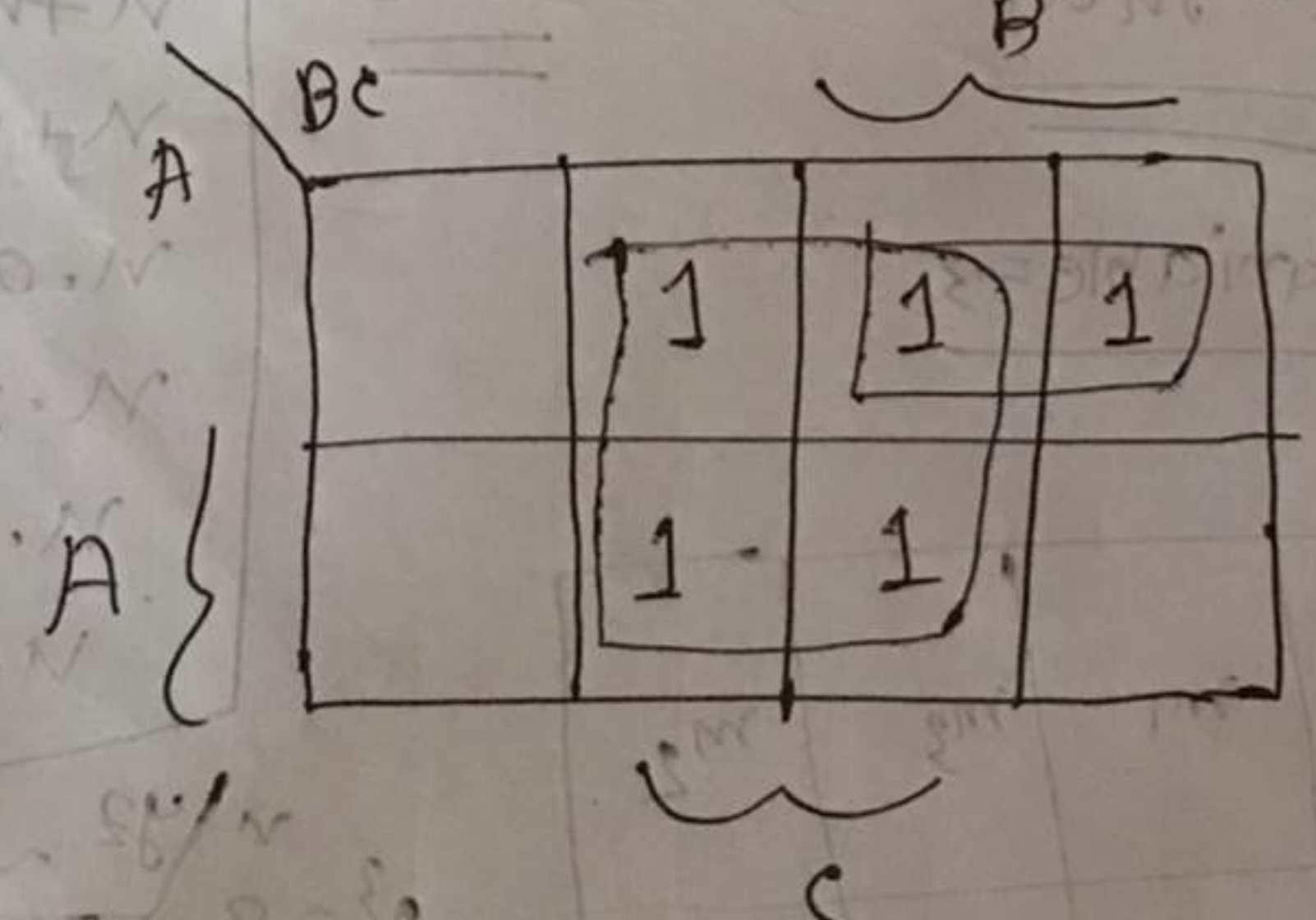
Example: ①  $F = x'y'z + x'yz' + xy'z' + xyz$



$F = x'y + xy'$

Standard form

Example: ②  $F = A'C + A'B + AB'C + BC$



$F = C + A'B$

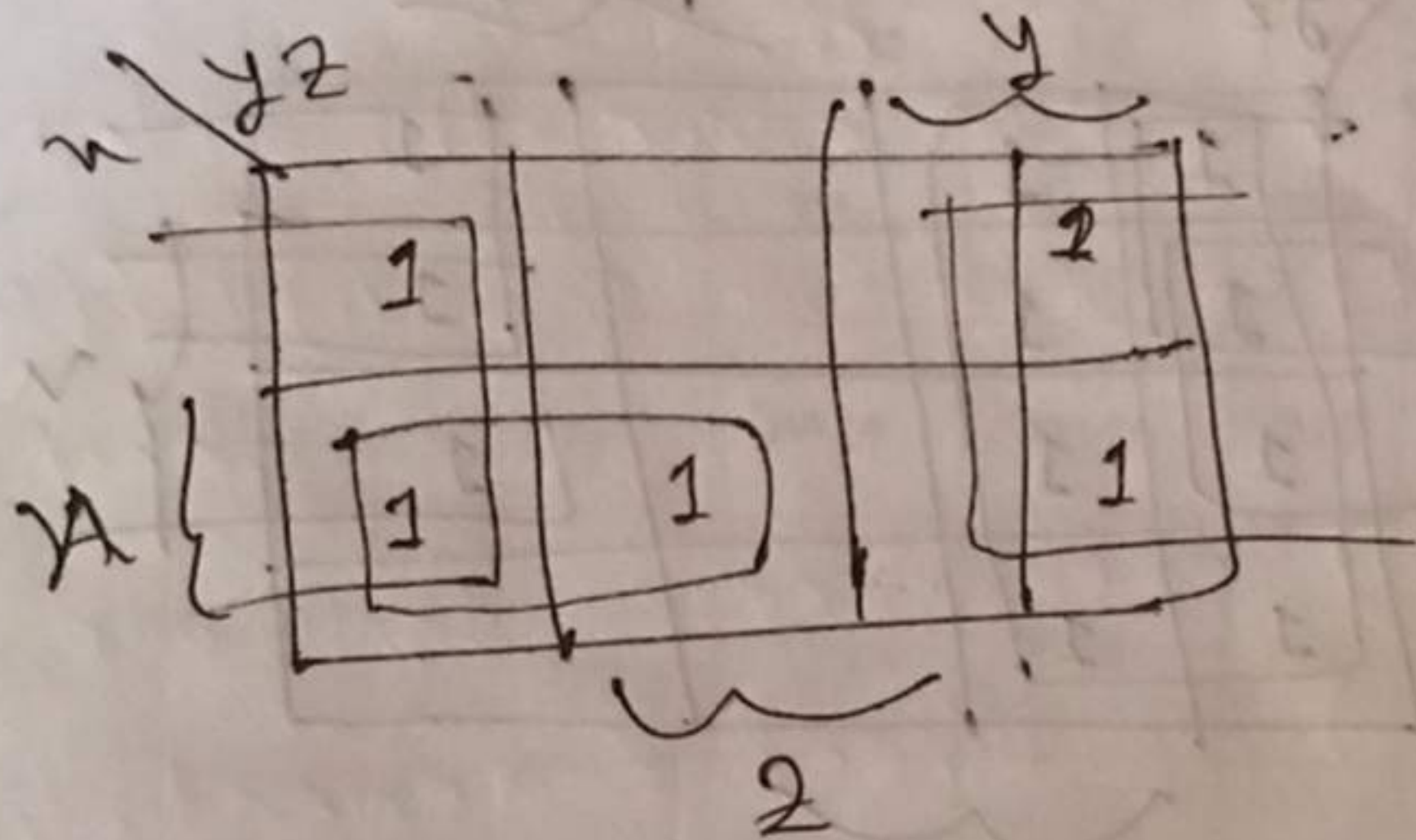
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Canonical form

Example: 3

$$F(x, y, z) = \sum (0, 2, 4, 5, 6)$$

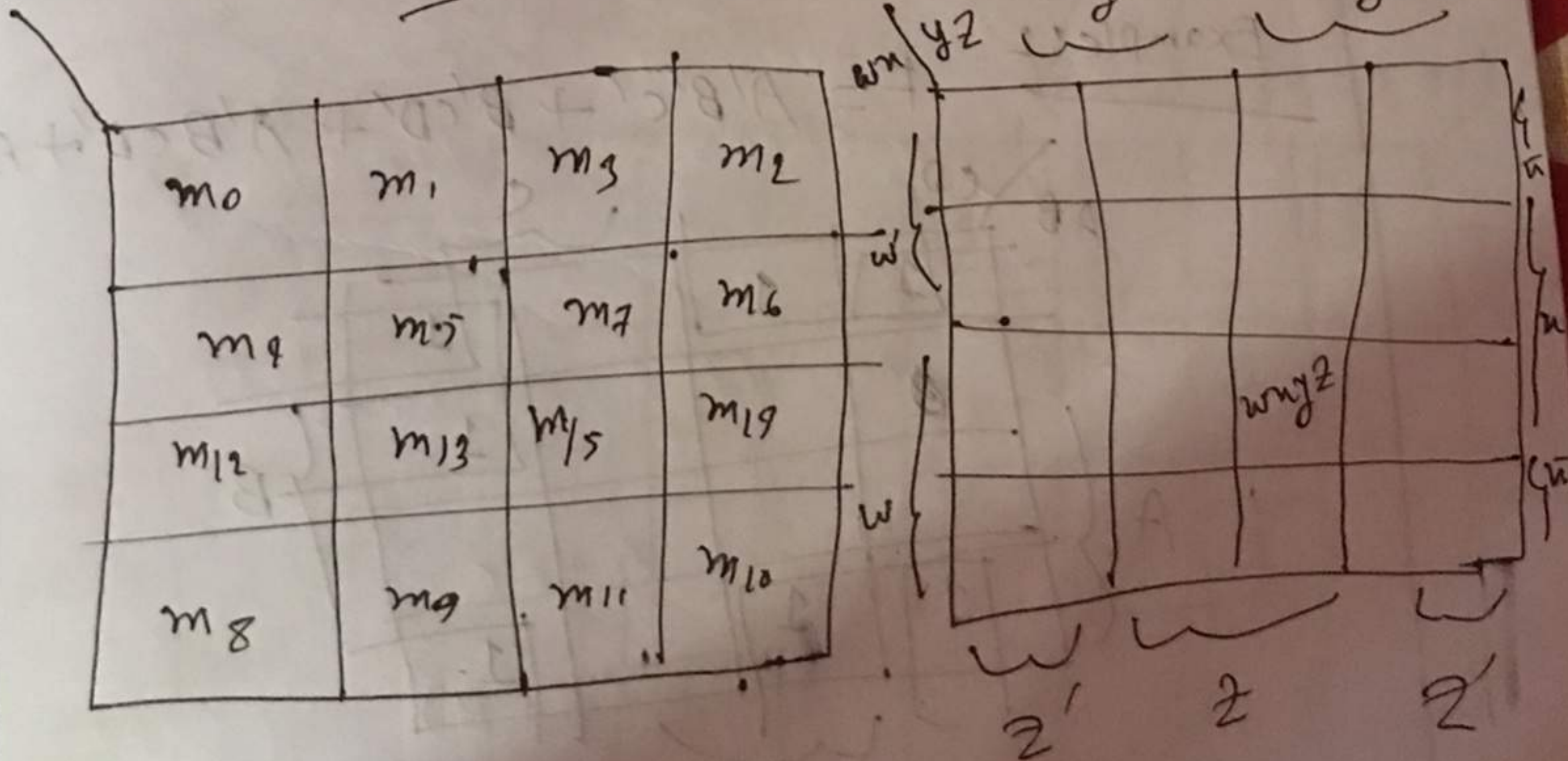


$$F = z' + xy'$$

4 variable

$$2^4 = 16$$

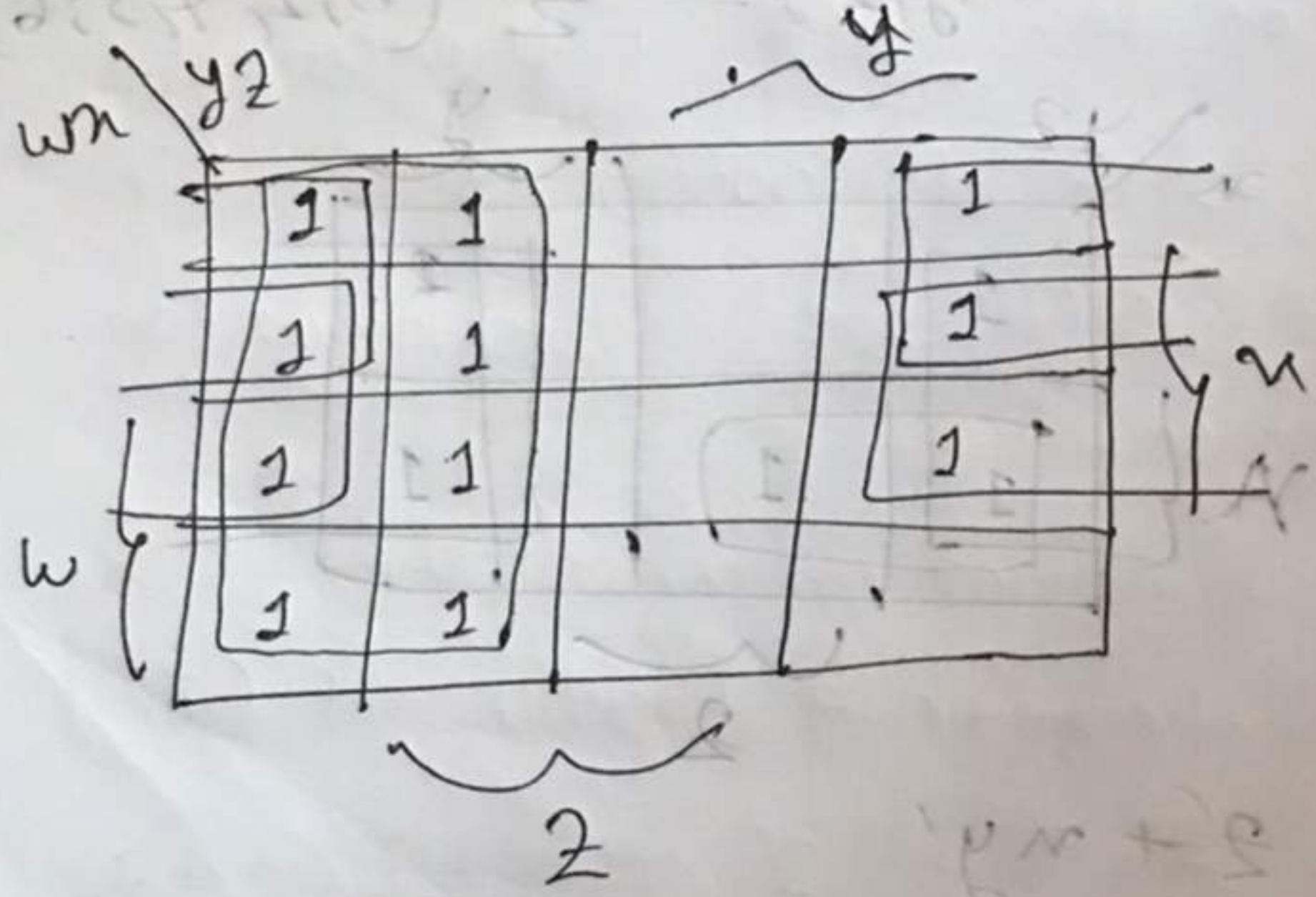
xyz



canonical form

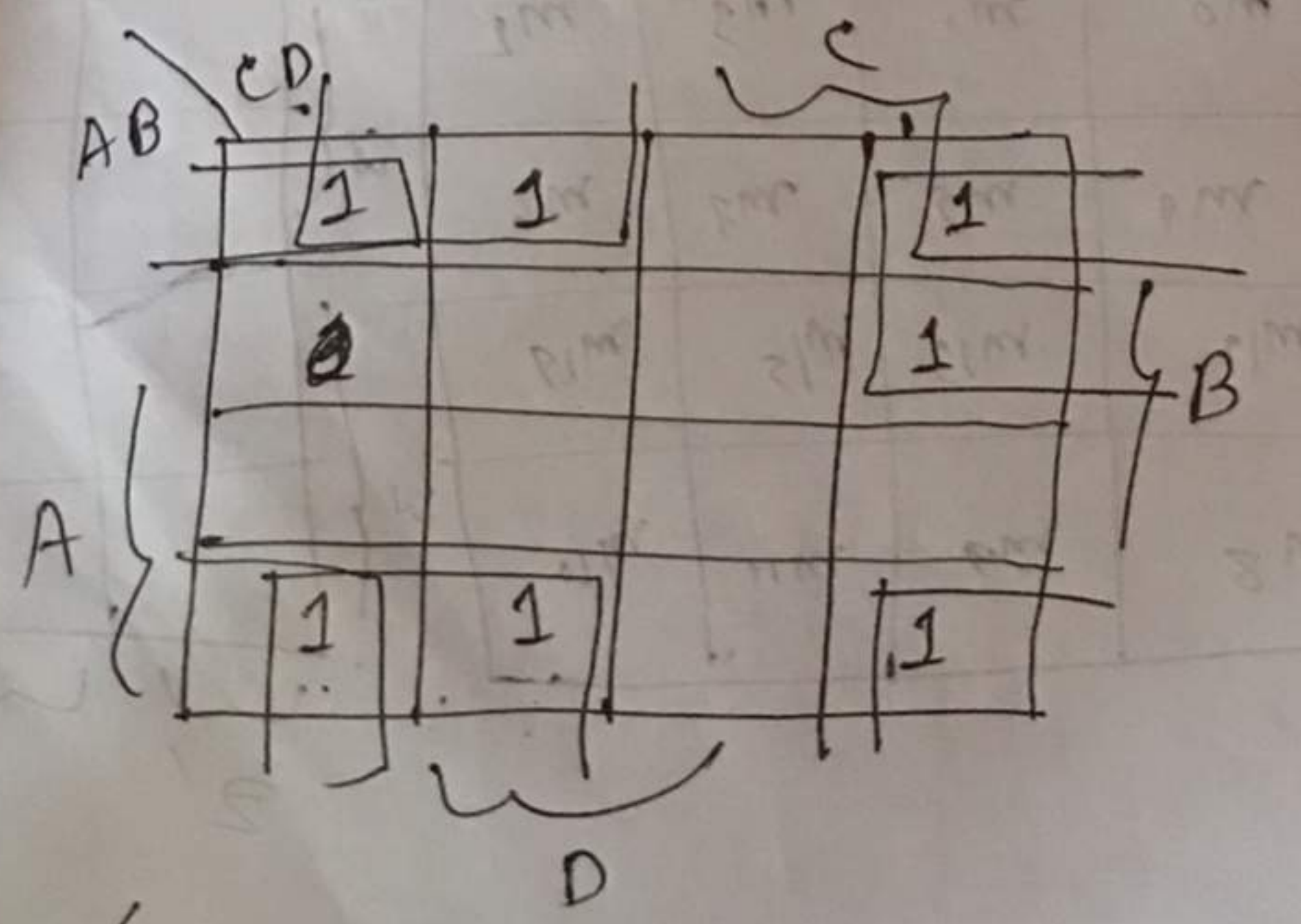
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Example: 1  $f(w, x, y, z) = \sum (0, 1, 2, 4, 5, 6, 8, 9, 12, 13, 14)$



$$F = y' + w'z' + xz'$$

Example: 2  $F = A'B'C' + B'CD' + A'BCD' + ABC'$



$$F = B'C' + B'D' + A'CD'$$



5 Variable

		$A'B'CDE'$				$A'B'C'D'E'$			
	$AB$	$CDE$ 000	$C'D'E'$ 001	$C'DE$ 011	$C'DE'$ 010	$CDE'$ 110	$CDE$ 111	$C'D'E$ 101	$CD'E'$ 100
$A'B'00$	$A'B'CD'$ $m_0E'$	$m_1$	$m_3$	$m_2$	$m_6$	$m_7$	$m_5$	$m_4$	
$A'B'01$	$m_8$	$m_9$	$m_{11}$	$m_{10}$	$A'BCDE'$ $m_{14}$	$m_{15}$	$m_{13}$	$m_{12}$	
$AB11$	$m_{24}$	$m_{25}$	$m_{27}$	$m_{26}$	$m_{30}$	$m_{31}$	$m_{29}$	$m_{28}$	
$AB'10$	$m_{16}$	$m_{17}$	$m_{19}$	$m_{18}$	$m_{22}$	$m_{23}$	$m_{21}$	$m_{20}$	

$2^5 = 32$

Example: ①

$F(A, B, C, D, E) = \sum (0, 2, 4, 6, 9, 11, 13, 15, 17, 21, 25, 27, 29, 31)$

	$AB$	$CDE$ 00	$01$	$11$	$10$				
$A'B'$	$A'B'$	1			1	1			1
$A'B$	$A'B$		1	1		1	1		
$AB$	$AB$		1	1		1	1		
$AB'$	$AB'$		1				1		

$C'D'E'$   $C'D'E$   $C'DE$   $C'DE'$   $CDE'$   $CDE$   $CD'E$   $CD'E'$

$F = BE + A'B'E' + AD'E$

Ans?

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Q) List Limitation of k-map?

- i) Scalability
- ii) Visual complexity
- iii) Human error
- iv) Limited to Binary Logic
- v) Complex functions
- vi) Difficulty with don't cares
- vii) Dependence on completeness
- viii) No Direct Implementation.

Sum of product / minterms  
product of sum / maxterms

$$\begin{aligned} \text{minterms} &= x'y'z' \\ \text{maxterms} &= x+y+z \end{aligned}$$

sum of product / minterms:

$$\begin{aligned} F &= A + B'C \\ A &= A(B + \bar{B}) \quad [B + \bar{B} = 1] \\ \Rightarrow A &= AB + A\bar{B} \\ \Rightarrow A &= AB(c + \bar{c}) + A\bar{B}(c + \bar{c}) \end{aligned}$$

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$$\rightarrow A = ABC + AB\bar{C} + A\bar{B}C + A\bar{B}\bar{C}$$

$$\rightarrow \bar{B}\bar{C} = \bar{B}\bar{C}(A + \bar{A})$$
$$\Rightarrow A\bar{B}\bar{C} + \bar{A}\bar{B}\bar{C}$$

$$F = A + \bar{B}\bar{C}$$

$$= ABC + AB\bar{C} + A\bar{B}C + A\bar{B}\bar{C} + \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}\bar{C}$$

$$= ABC + AB\bar{C} + A\bar{B}C + \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}\bar{C}$$

$$= m_7 + m_6 + m_5 + m_4 + m_1$$

[ $u+u=u$ ]

$$F(A, B, C) = \sum (1, 4, 5, 6, 7) \underline{\underline{Q}}$$

product of sum / max terms

$$F = xy + xz$$

$$= (x + xz)(y + xz)$$

$$= (x + x')(x + z)(y + x')(y + z)$$

$$\cancel{x + x'} = \cancel{x + x' + y \cdot y} \quad [y \cdot \bar{y} = 0]$$

$$= (x + x' + y)(x + x' + y')$$

$$\cancel{x+2} = \cancel{x+2} \cdot (y+x) (y+z)$$

$$x+2 = \overbrace{x+2+y \cdot y} \cdot [y \cdot y = 0]$$

$$= (x+2+y)(x+2+y)$$

$$y+x' = y+x' + z \cdot z$$

$$= (y+x'+z)(y+x'+z)$$

$$y+z = y+z + n \cdot \bar{n}$$

$$= (y+z+n)(y+z+\bar{n})$$

$$F = (x+y+z)(x+y+z)(\bar{n}+y+z)(\bar{n}+y+z)$$

$$(x+y+z) (\bar{n}+y+z)$$

$$= (x+y+z)(x+y+z)(\bar{n}+y+z)(\bar{n}+y+z)$$

$$= m_0 \cdot m_2 \cdot m_9 \cdot m_5$$

$$F(x,y,z) = \prod (0, 2, 4, 5)$$

⑤ Simplify the following Boolean function D in product of sum -

$$\Rightarrow D = BDE' + CD'E'$$

~~$$D = (BDE' + BCD'E')$$~~

~~$$\Rightarrow D = BDE' +$$~~

Solve :  $D = BDE' + CD'E'$

$$\Rightarrow D = (B + CD'E') (D + CD'E') (E' + CD'E')$$

$$\Rightarrow D = (B + C) (B + D') (B + E') (D + C) (D + D') (D + E') (E' + C) (E' + D') (E' + E')$$

$$B + C = B + C + A\bar{A} \Rightarrow D = (B + C) (B + D') (B + E') (D + C) (D + E') (E' + C) (E' + D') \cdot E'$$

$$B + C + A = (B + C + A)$$

$$B + C + A = B + C + A + D\bar{D}$$

$$= (B + C + A + D)$$

$$(B + C + A + \bar{D})$$

$$B + C + A + \bar{D} = B + C + A + \bar{D} + E\bar{E}$$

$$= (B + C + A + \bar{D} + E)$$

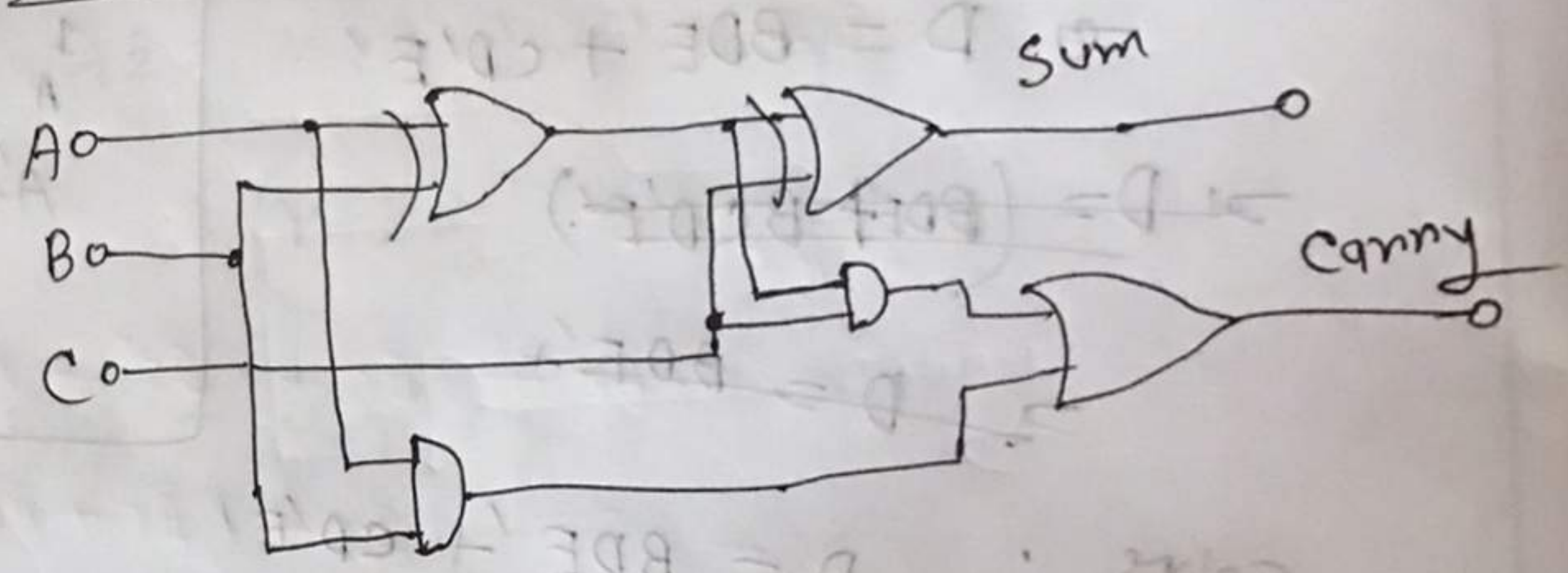
$$(B + C + A + \bar{D} + \bar{E})$$

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A	B	C	
1	1	1	⑥
1	1	0	
A	B	C	$\Rightarrow m_6$
A'	B'	C	$\Rightarrow M_6$

⑥ Design a Full adder?

Circuit Diagram:-



For sum:  $sum = \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}\bar{C} + ABC$   
 $= \bar{A}(\bar{B}C + B\bar{C}) + A(\bar{B}\bar{C} + BC)$   
 $= \bar{A}(B \oplus C) + A(\bar{B} \oplus \bar{C})$

For carry:  $carry = \bar{A}BC + A\bar{B}C + AB\bar{C} + ABC$   
 $= C(\bar{A}B + AB) + AB(\bar{C} + C)$   
 $= C(A \oplus B) + AB$

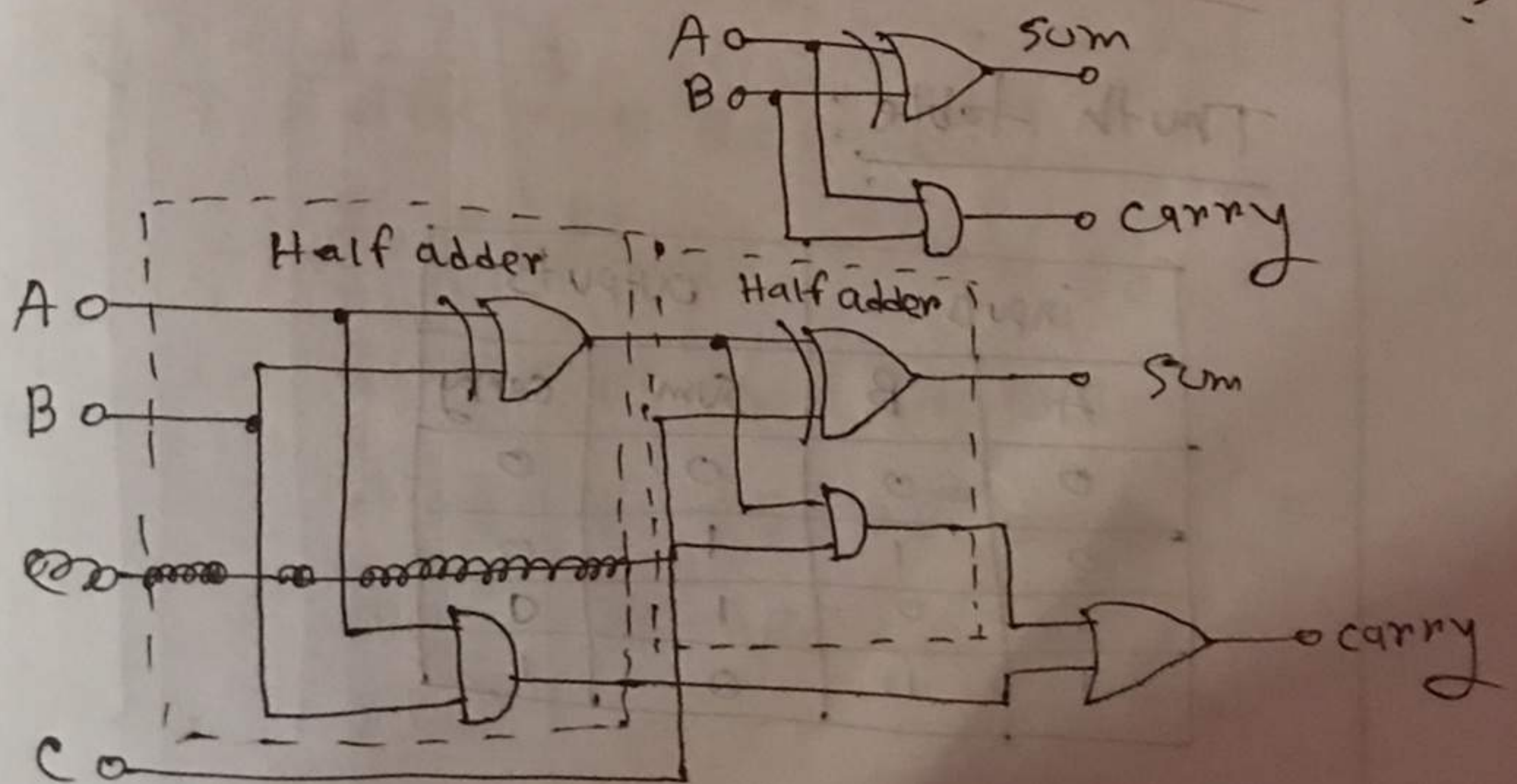
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Truth table :

inputs			outputs	
A	B	C	Sum	Carry
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

⑦ Draw a Full adder using two half adder?



Carry

ABC

(A+B+C)

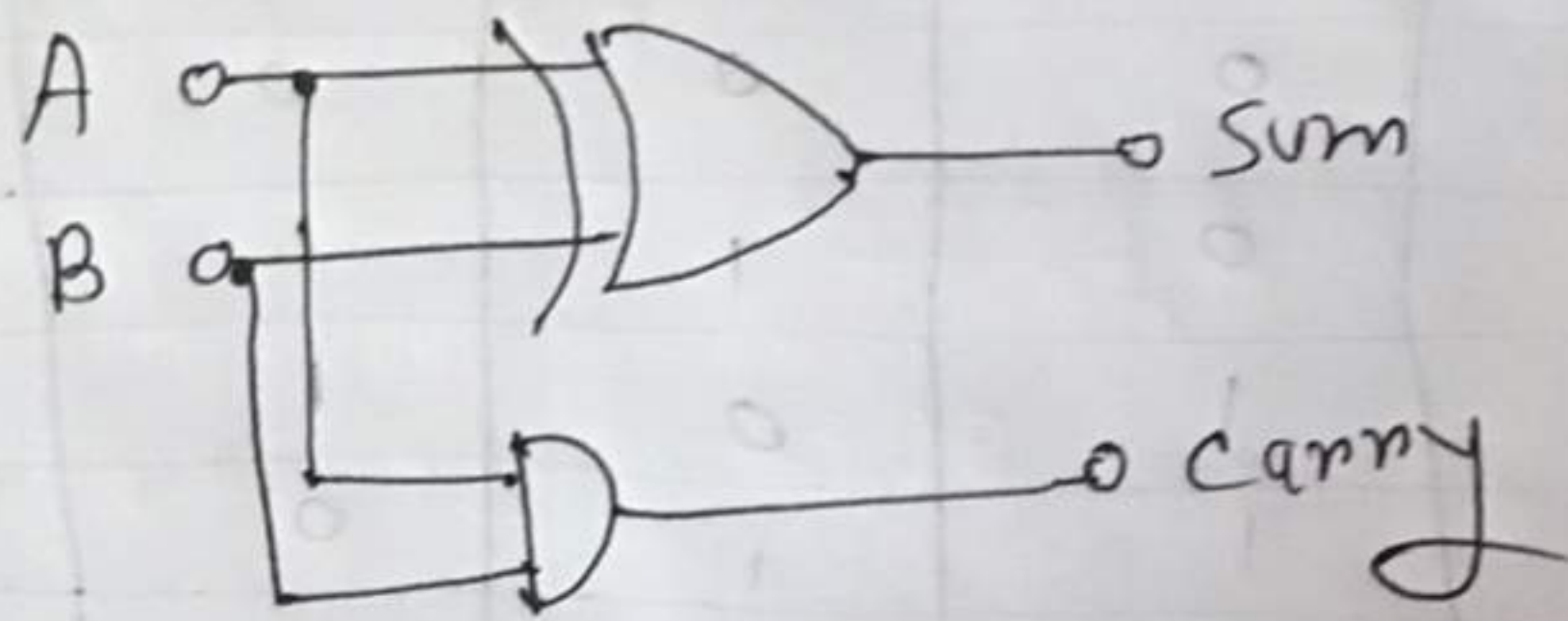
(C)

(C+ABC)

(C+C)

② Design Half adder ?

Circuit Diagram:



For Sum:  $Sum = \bar{A}B + A\bar{B}$   
 $= A \oplus B$

For Carry:  $Carry = AB$

Truth table:

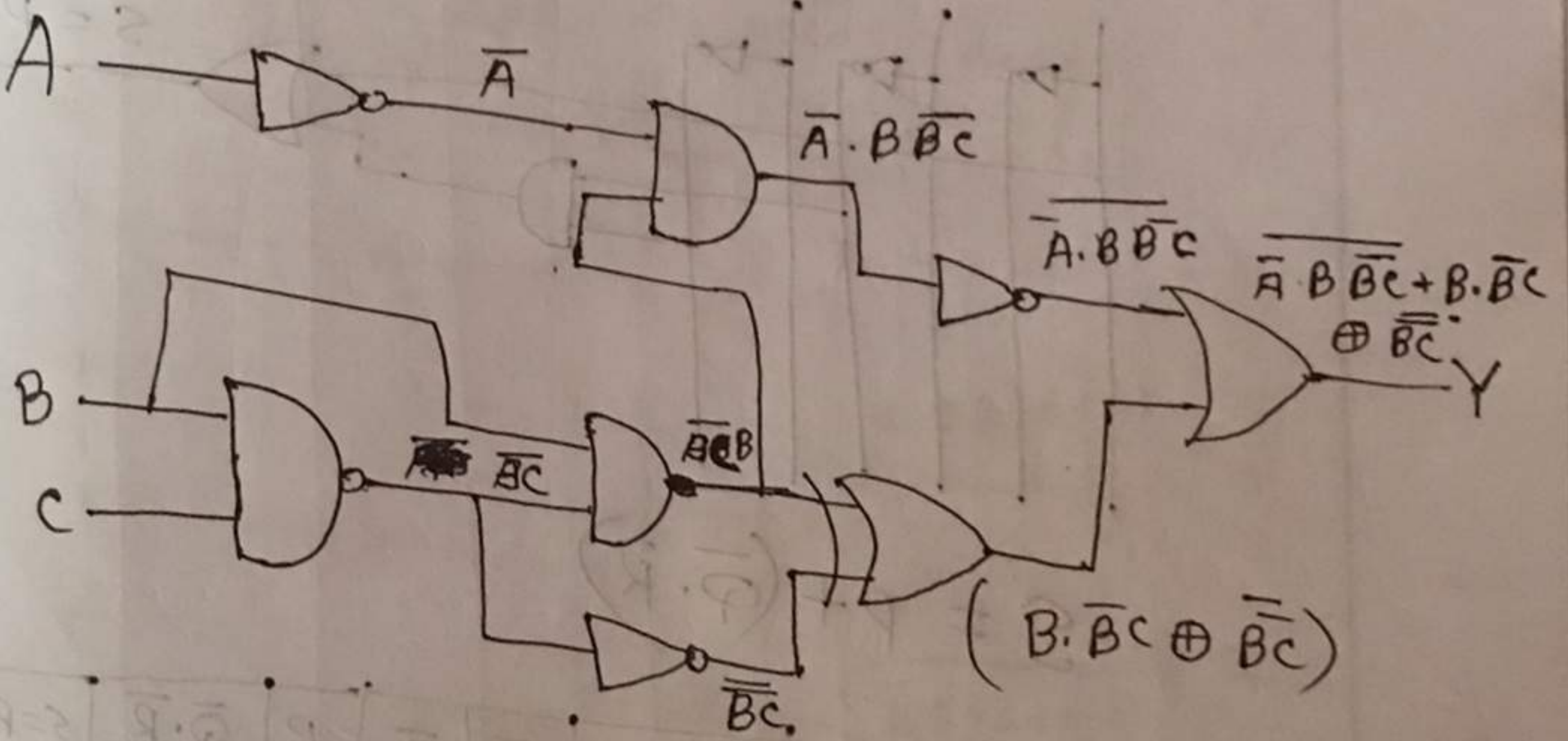
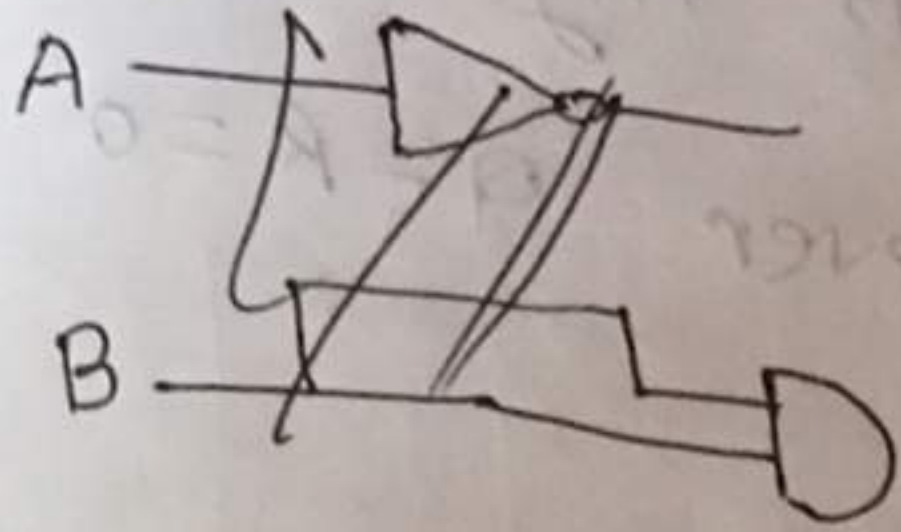
inputs		outputs	
A	B	Sum	Carry
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1



Subject: \_\_\_\_\_

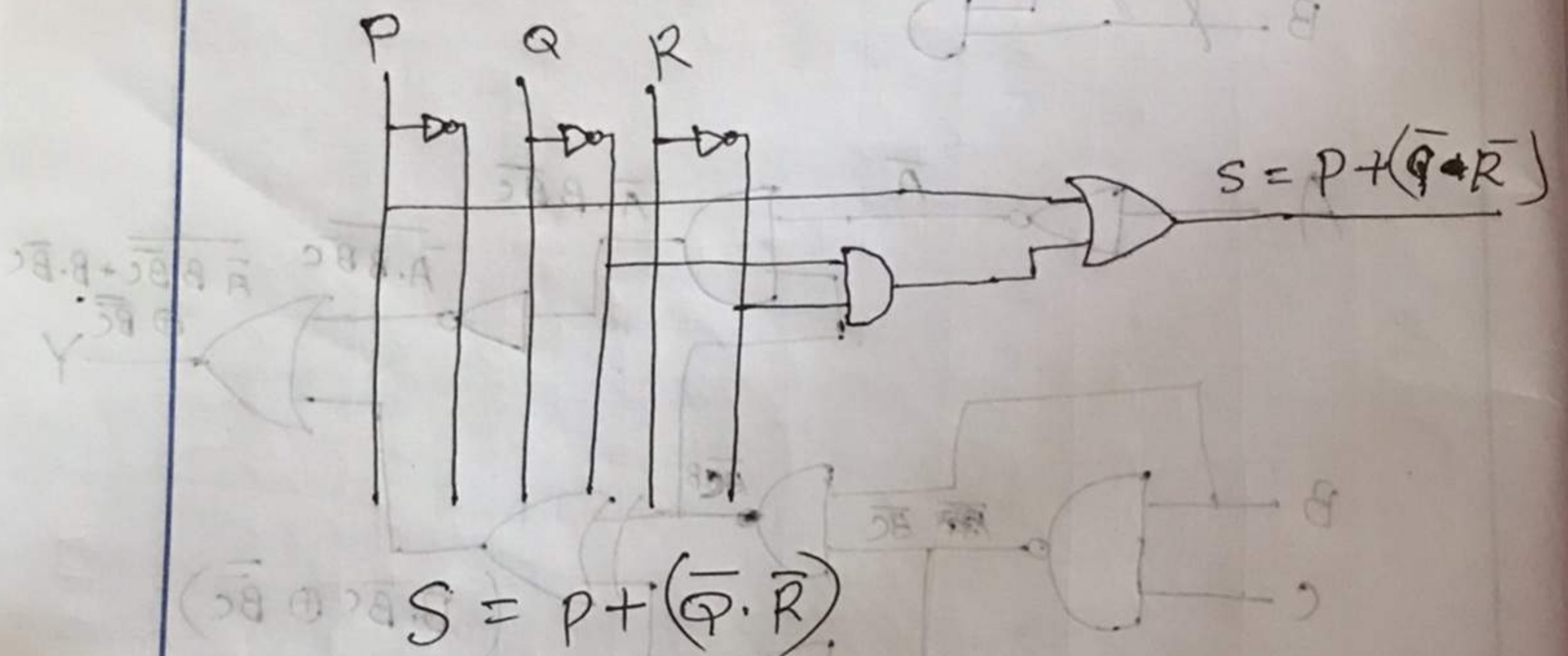
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8) Simplify the logic circuit?



$$\begin{aligned} Y &= \overline{A} B \overline{B} C + (B \cdot \overline{B} C \oplus \overline{B} C) \\ &= \overline{A} + \overline{B} + \overline{B} C + \{B(\overline{B} + C) \oplus B C\} \\ &= A + \overline{B} + B C + (B \overline{B} + B \overline{C} \oplus B C) \\ &= A + \overline{B} + B C + (B \overline{C} \oplus \overline{B} C) \\ &= A + \overline{B} + B C + (B \overline{C} \oplus B C) \end{aligned}$$

9) Design a logic circuit with input P, Q, R so that output S is High whenever P is "1" or whenever Q=R=0

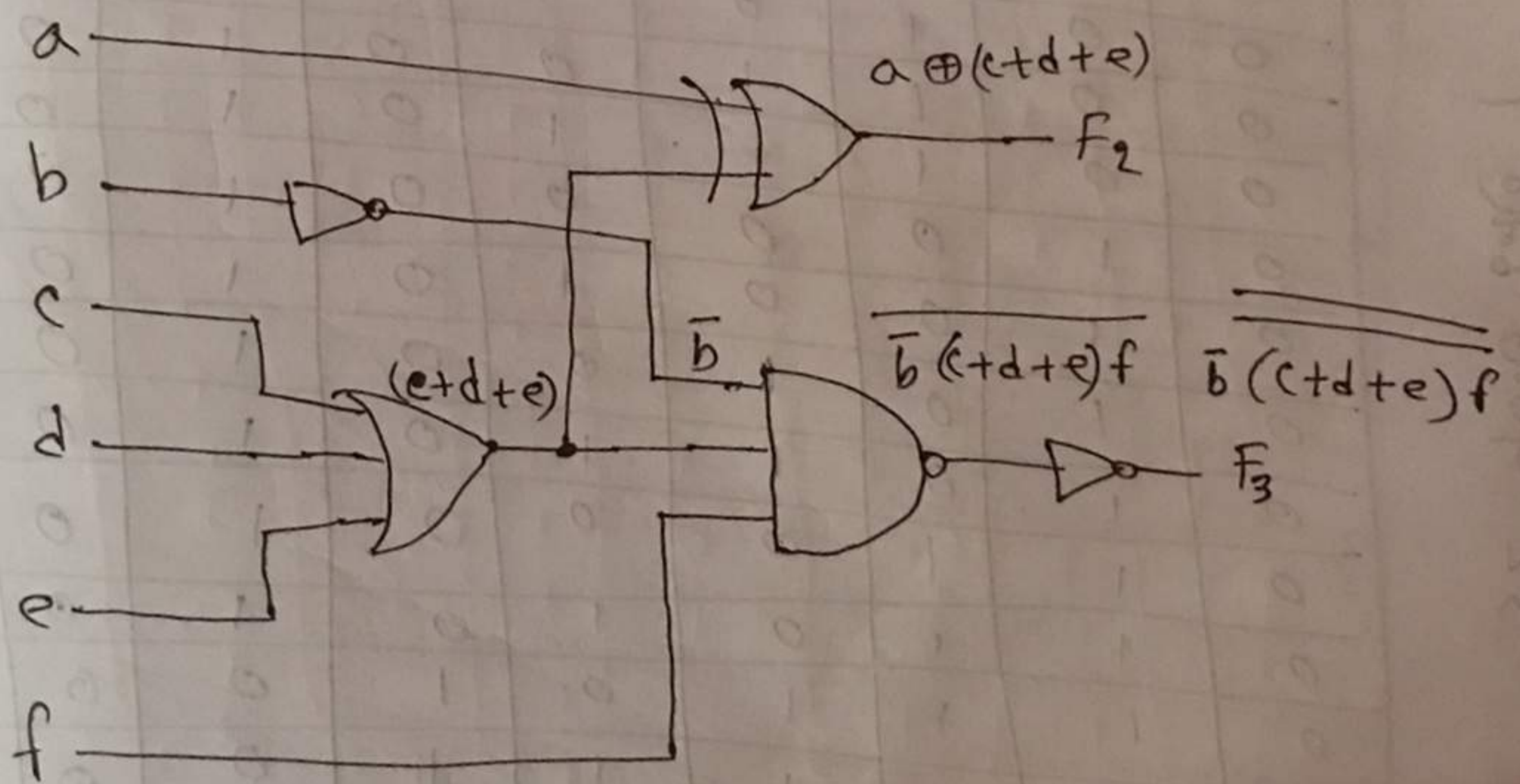
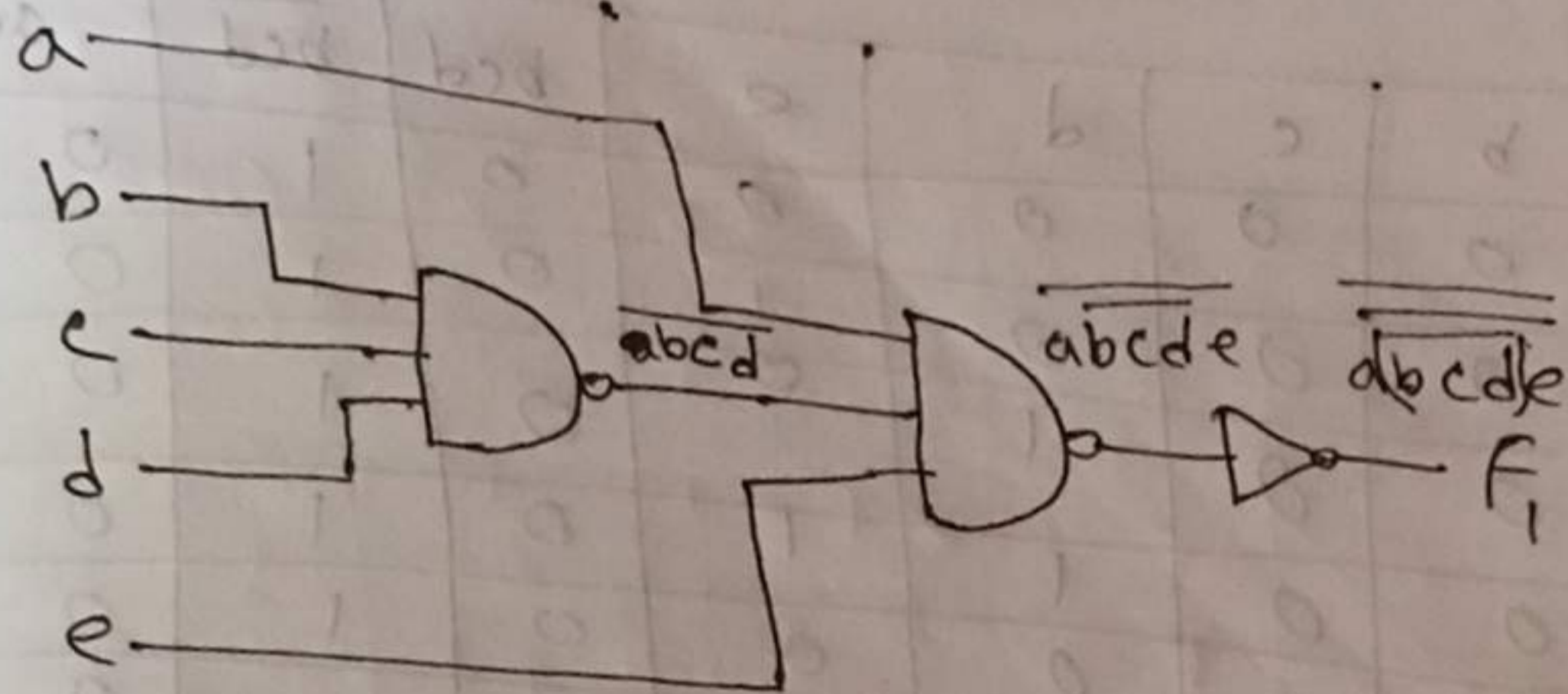


	P	Q	R	$\bar{Q}$	$\bar{R}$	$P$	$\bar{Q} \cdot \bar{R}$	$S = P + (\bar{Q} \cdot \bar{R})$
→	0	0	0	1	1	0	1	1
	0	0	1	1	0	0	0	0
	0	1	0	0	1	0	0	0
	0	1	1	0	0	0	0	0
→	1	0	0	1	1	1	1	1
→	1	0	1	1	0	1	0	1
→	1	1	0	0	1	1	0	1
→	1	1	1	0	0	1	0	1

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10) Write Boolean expressions and construct the truth tables describing the outputs of the circuits described by the following logic diagrams?



$$F_1 = \overline{abcde}$$

$$\neg F_1 = abcde = ae \overline{bcd}$$

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a	b	c	d	e	bcd	$\overline{bcd}$	ae	$\overline{bcd}ae$
0	0	0	0	0	0	1	0	0
0	0	0	0	1	0	1	0	0
0	0	0	1	0	0	1	0	0
0	0	0	1	1	0	1	0	0
0	0	1	0	0	0	1	0	0
0	0	1	0	1	0	1	0	0
0	0	1	1	0	0	1	0	0
0	0	1	1	1	0	1	0	0
0	1	0	0	0	0	1	0	0
0	1	0	0	1	0	1	0	0
0	1	0	1	0	0	1	0	0
0	1	0	1	1	0	1	0	0
0	1	1	0	0	0	1	0	0
0	1	1	0	1	0	1	0	0
0	1	1	1	0	0	1	0	0
0	1	1	1	1	0	1	0	0
1	0	0	0	0	0	0	0	0
1	0	0	0	1	0	0	0	0
1	0	0	1	0	0	0	0	0
1	0	0	1	1	0	0	0	0
1	0	1	0	0	0	0	0	0
1	0	1	0	1	0	0	0	0
1	0	1	1	0	0	0	0	0
1	0	1	1	1	0	0	0	0
1	1	0	0	0	1	0	0	0
1	1	0	0	1	1	0	0	0
1	1	0	1	0	1	0	0	0
1	1	0	1	1	1	0	0	0
1	1	1	0	0	1	0	0	0
1	1	1	0	1	1	0	0	0
1	1	1	1	0	1	0	0	0
1	1	1	1	1	1	0	0	0

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$$F_2 = a \oplus (c t d t e)$$

a	c	d	e	c t d t e	$a \oplus (c t d t e)$
0	0	0	0	0	0
0	0	0	1	1	1
0	0	1	0	1	1
0	0	1	1	1	1
0	1	0	0	1	1
0	1	0	1	1	1
0	1	1	0	1	1
0	1	1	1	1	1
1	0	0	0	0	1
1	0	0	1	1	0
1	0	1	0	1	0
1	0	1	1	1	0
1	1	0	0	1	0
1	1	0	1	1	0
1	1	1	0	1	0
1	1	1	1	1	0

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$$F_2 = \overline{\overline{b} (c+d+e) f}$$

$$\Rightarrow F_3 = \overline{b} f (c+d+e)$$

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b	c	d	e	f	$\overline{b}$	$\overline{b}f$	c+d+e	$\overline{b}f(c+d+e)$
0	0	0	0	0	1	0	0	0
0	0	0	0	1	1	1	0	0
0	0	0	1	0	1	0	1	0
0	0	0	1	1	1	1	1	1
0	0	1	0	0	1	0	1	0
0	0	1	0	1	1	1	1	1
0	0	1	1	0	1	0	1	0
0	0	1	1	1	1	1	1	1
0	1	0	0	0	1	0	1	0
0	1	0	0	1	1	1	1	1
0	1	0	1	0	1	0	1	0
0	1	0	1	1	1	1	1	1
1	0	0	0	0	0	0	0	0
1	0	0	0	1	0	0	0	0
1	0	0	1	0	0	0	1	0
1	0	0	1	1	0	0	1	0

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① Show that a positive logic NAND gate is a negative logic NOR gate and vice versa.

Definitions:

1) positive Logic: i) Logic Level '1' (true) is represented by a high voltage

ii) Logic Level '0' (false) is represented by a low voltage.

2) negative Logic: i) Logic Level '1' (true) is represented by a low voltage.

ii) Logic Level '0' (false) is represented by a high voltage.

NAND gate:  $P = \overline{A \cdot B}$

NOR gate:  $P = \overline{A + B}$

NAND gate (positive)

A	B	AB	$\overline{AB}$
0	0	0	1
0	1	0	1
1	0	0	1
1	1	1	0

In positive  
The output is high (1) for all combinations of inputs except when both inputs are high (1)

NOR gate (negative)

A	B	$\overline{A+B}$
1	1	0
1	0	1
0	1	1
0	0	1

In negative,  
The output is low (0) only when both inputs are high (1).

For NAND gate in positive logic:

When both inputs are low (0), the output is high (1), and when both inputs are high (1), the output is low (0).



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## For NOR gate in negative logic:

When both inputs are high (1), the output is low (0), and when both inputs are ~~high (1)~~, low (0), the output is high (1).

Thus, we can see that a positive logic NAND gate behaves like a negative logic NOR gate and vice versa.

Extra:

AND (positive)

A	B	AB
0	0	0
0	1	0
1	0	0
1	1	1

AND (negative)

A	B	$\overline{AB}$
1	1	0
1	0	1
0	1	1
0	0	1

NAND (positive)

A	B	$\overline{AB}$
0	0	1
0	1	1
1	0	1
1	1	0

NAND (negative)

A	B	$\overline{AB}$
1	1	0
1	0	0
0	1	0
0	0	1

OR (positive)

A	B	A+B
0	0	0
0	1	1
1	0	1
1	1	1

OR (negative)

A	B	A+B
1	1	1
1	0	0
0	1	0
0	0	0

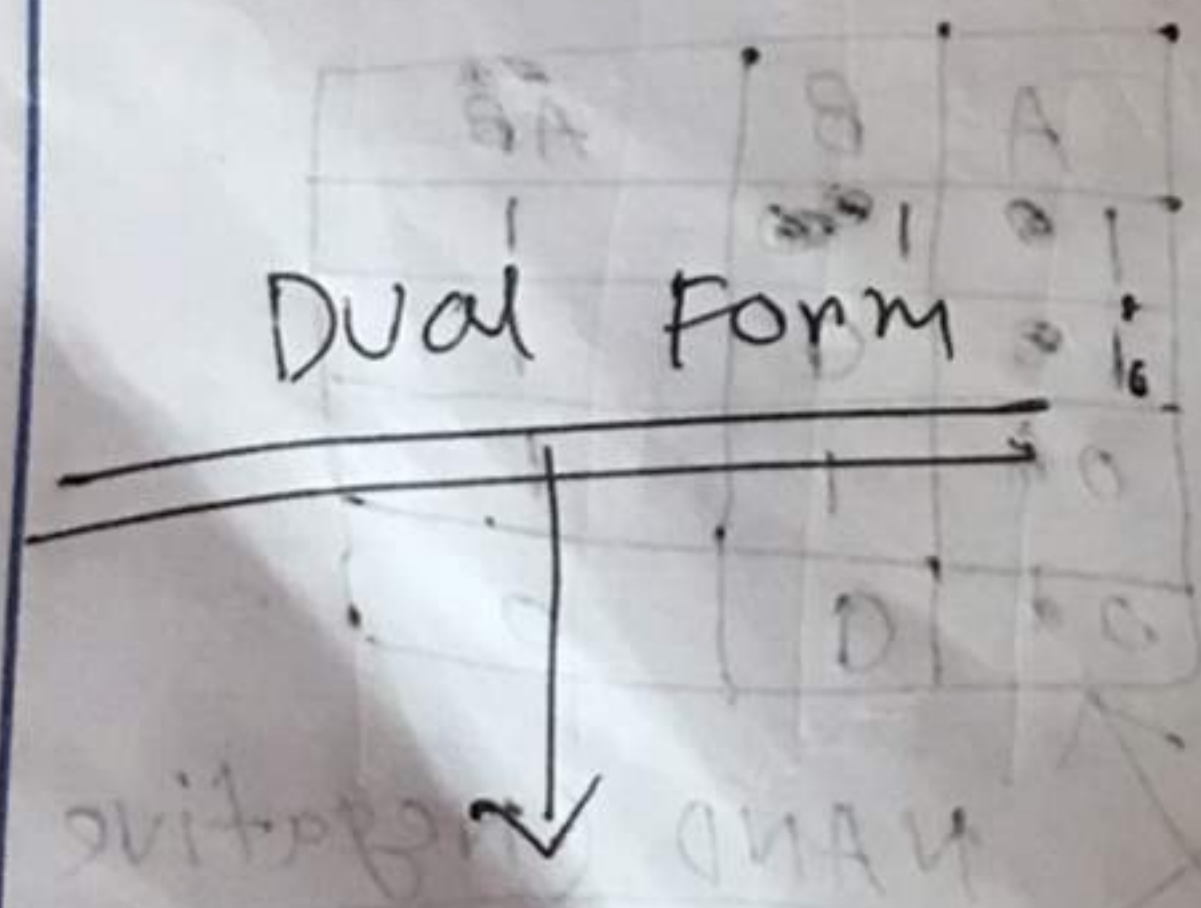
NOR (positive)

A	B	$\overline{A+B}$
0	0	1
0	1	0
1	0	0
1	1	0

NOR (negative)

A	B	$\overline{A+B}$
1	1	0
1	0	1
0	1	1
0	0	1

Dual Form



AB (positive) → AB (negative) or A+B (positive)

A+B (positive) → A+B (negative) or AB (positive)

BA	A	B	A
0	1	0	0
0	0	1	0
0	1	0	1
1	0	0	1

Subject: \_\_\_\_\_

Date: \_\_\_\_\_

(12) Show that the dual form of the XOR is also its complement?

Soln:  $x \oplus y = xy' + x'y$

$$\text{Complement} = (x \oplus y)' = (xy' + x'y)'$$

$$= \overline{xy' + x'y}$$

$$= \overline{xy'} \overline{x'y}$$

$$= (x' + y)(x + y')$$

$$\text{Dual of } (x \oplus y) = \text{dual of } (xy' + x'y)$$

$$= (x + y')(x' + y)$$

$$= (x' + y)(x + y')$$

$$\therefore (x \oplus y)' = \text{Dual of } (x \oplus y)$$

Subject: \_\_\_\_\_

Date: \_\_\_\_\_

Q1) Implement the following Boolean expression with Exclusive-OR and AND gate?

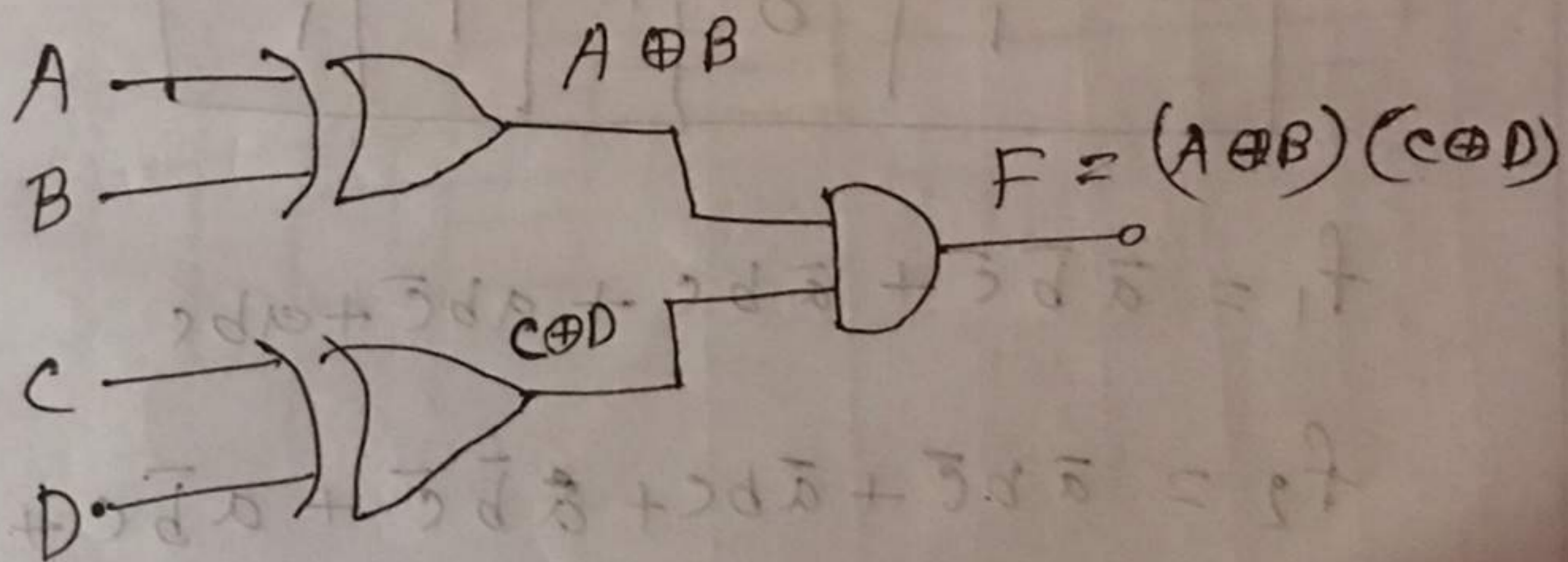
$$F = \underline{AB'CD'} + \underline{A'BCD'} + \underline{AB'C'D} + \underline{A'BC'D}$$

$$\Rightarrow F = C'D'(AB' + A'B) + C'D(AB' + A'B)$$

~~$$\Rightarrow F = (A'B + AB')$$~~

$$\Rightarrow F = (AB' + A'B)(C'D' + C'D)$$

$$\Rightarrow F = (A \oplus B)(C \oplus D)$$



19) write the Boolean expression and draw the logic circuit whose outputs are by the following truth table?

$f_1$	$f_2$	a	b	c
1	0	0	0	0
0	0	0	0	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	0	1
1	1	1	1	0
1	0	1	1	1

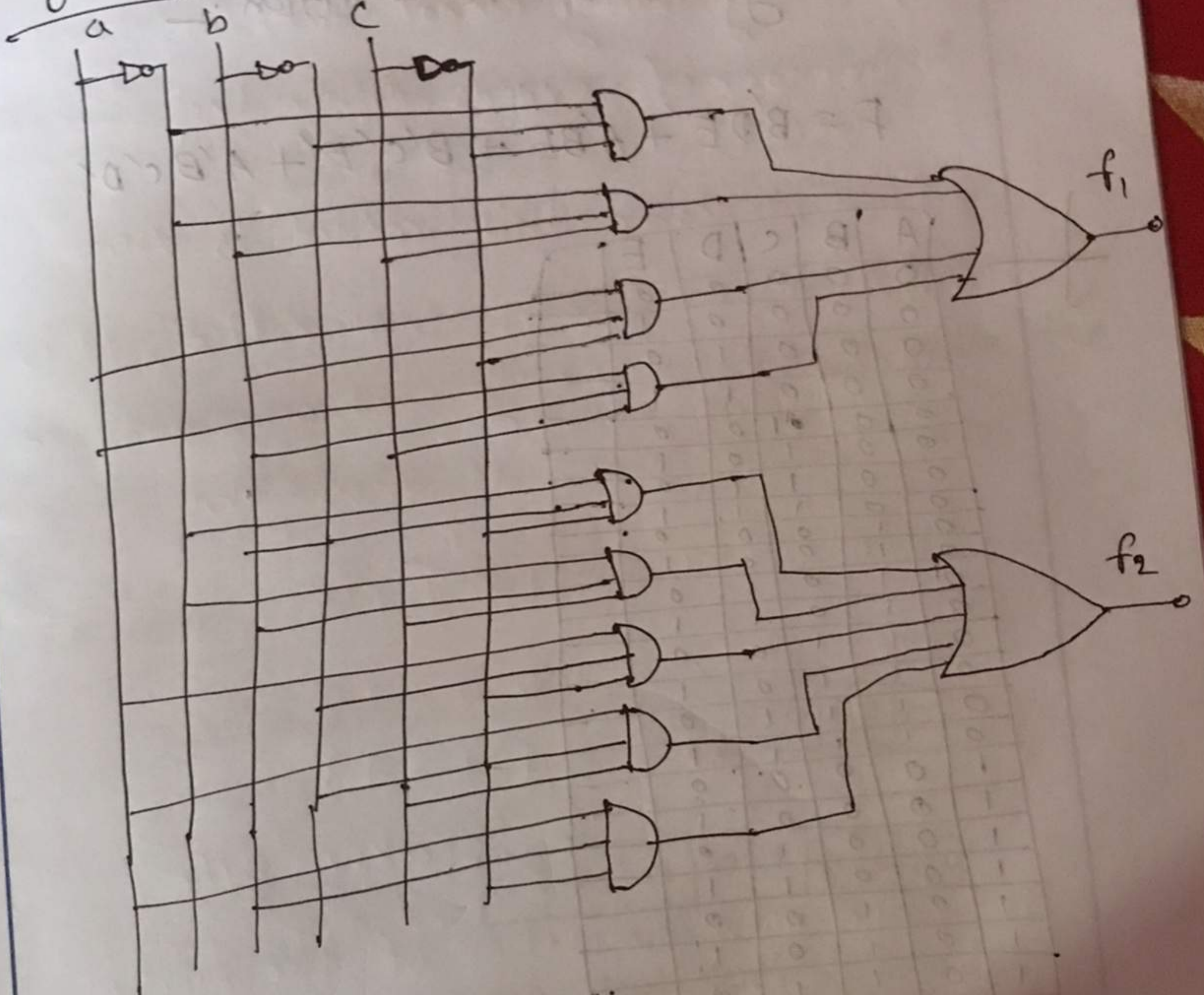
$$f_1 = \bar{a}\bar{b}\bar{c} + \bar{a}b\bar{c} + a\bar{b}\bar{c} + abc$$

$$f_2 = \bar{a}b\bar{c} + \bar{a}bc + a\bar{b}\bar{c} + a\bar{b}c + abc$$

Subject: \_\_\_\_\_

Date: \_\_\_\_\_

### Logic Diagram



Extra: K-Map (Don't care conditions)

transmission  
data with  
parity bit.

simplify the boolean function:  $F(w, x, y, z) =$

$$\sum (1, 3, 4, 11, 15)$$

$$d(w, x, y, z) = \sum (0, 2, 5)$$

		$y$		
$w/x$	$yz$			
	X	1	1	X
		X	1	
			1	
			1	

$w$  (bracketed on the left side of the table)  
 $z$  (bracketed under the last two columns of the table)

$$F = yz + w'z$$

[Combining 1's  
and x's]

NAND gate is a universal gate?

① A universal gate is a gate which can implement any Boolean function without need to use any other gate type. NOR and NAND gate is called universal gates because all the gates (NOT, AND, OR) can be created by using this gate.

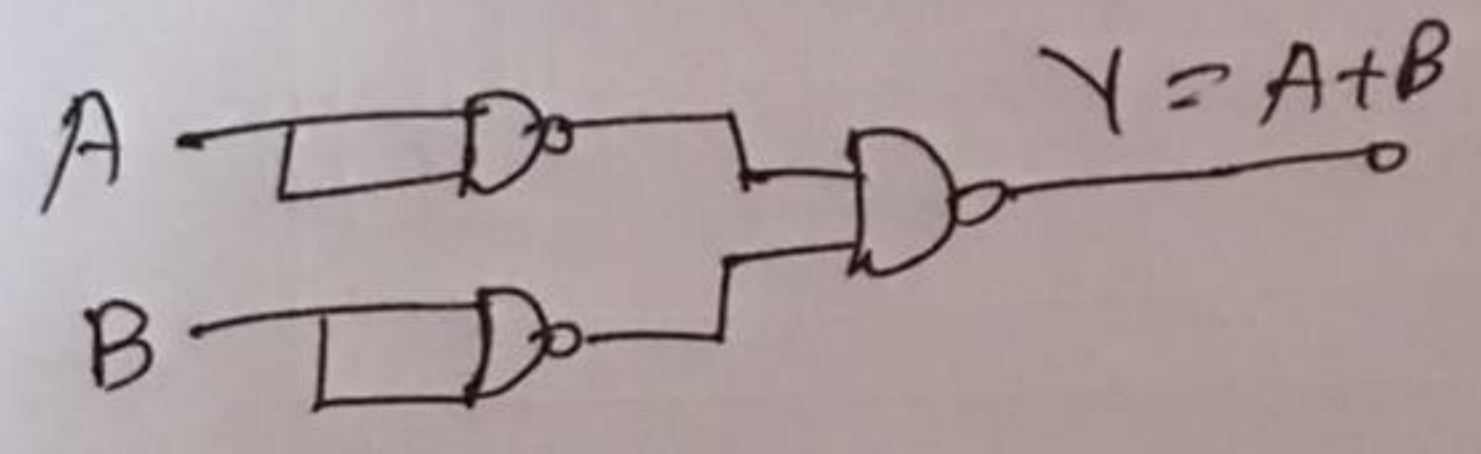
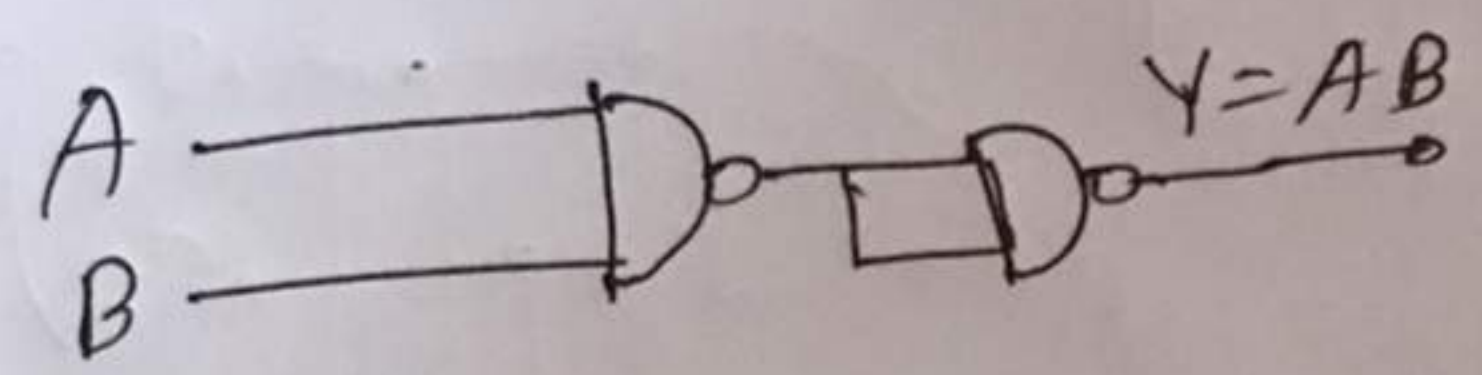
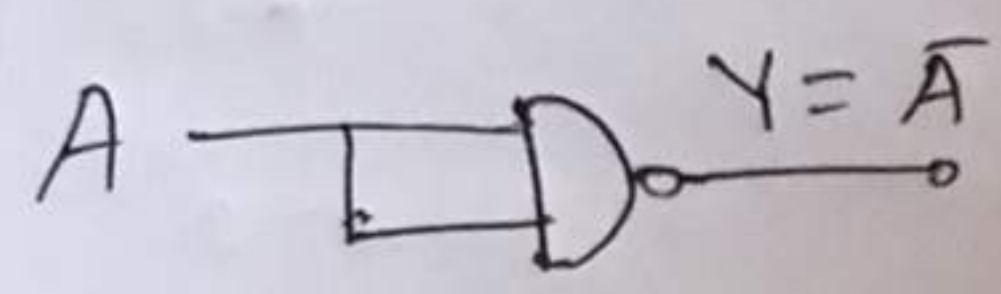




Implement :

NAND

NOR



NOR

