

## **Course Content**

### **Introduction**

- Introducing minerals
- Definition of mineral and mineraloid
- Conditions to be a mineral
- Definition of mineralogy

### **Scope**

### **Study of Physical and Chemical Properties of Minerals**

- **Physical Properties of Minerals**
  - Optical properties
    - Color
    - Diaphaneity
    - Luster
    - Streak
    - Luminescence
  - Crystal shape
    - Concepts of atomic bonds in forming mineral crystals
    - Crystal forms
      - Crystal systems
      - Vectorial properties of crystals
    - Crystal habits
      - Habits of single crystals
      - Habits of crystal aggregates
  - Properties regarding strength and breaking of minerals
    - Tenacity
    - Fracture, cleavage and parting
    - hardness
  - Density and specific gravity
  - Magnetism of minerals
  - Electric properties
  - Reaction to dilute hydrochloric acid
  - Twinning
  - Pseudomorphism
    - Metamict minerals
    - Polymorphism

- **Chemical Properties of Minerals**

- **Mineral chemistry**

- Composition of the Earth's crust
    - Methods of chemical analysis
    - Compositional variation in minerals
      - Solid solution
    - Graphical representation of mineral composition
    - *Mineral stability and phase diagrams*
      - *Mineral stability*
      - *Phase diagrams*
      - *Two component (binary) phase diagrams*
        - *Experimental determination of two component phase diagrams*
        - *Two component eutectic systems*
        - *Incongruent melting*
        - *Solid solution systems*
        - *Exsolution*

**Genesis of Minerals**

**Composition of the Earth's Crust**

**Classifications of Minerals**

**Environments of Mineral Formation**

**Study of Minerals with Emphasis on Rock-forming Minerals**

## Mineral Stability and Phase Diagrams

### Mineral Stability

As we discussed previously, there are four major processes by which minerals form. Each of these occurs within a limited range of environmental conditions. First, the chemical ingredients must be present, and second, the pressure and temperature conditions must be right. Let's first review these mineral forming processes and the pressure temperature conditions necessary.

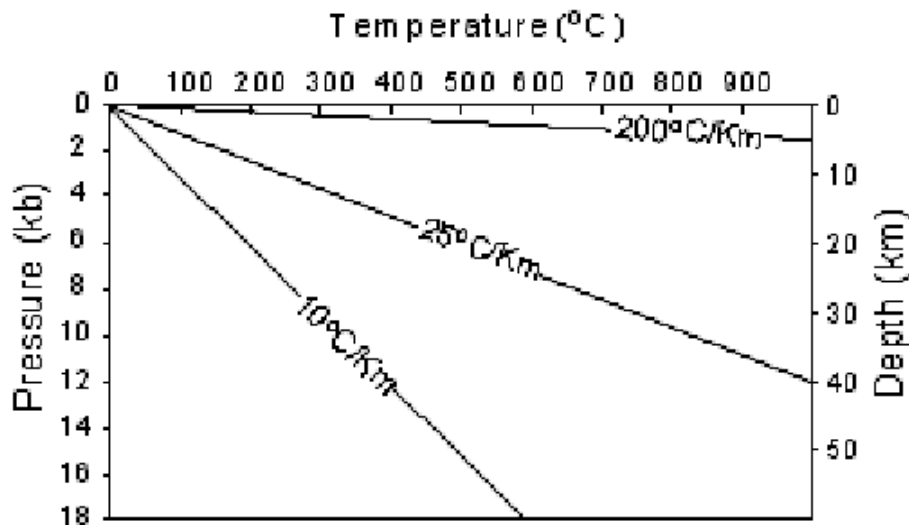
- Precipitation from a fluid like  $H_2O$  or  $CO_2$ .
  - Hydrothermal Processes -  $T = 100 - 500^{\circ}C$ ,  $P = 0$  to 1000 MPa (10 kb)
  - Diagenesis -  $T = 0 - 200^{\circ}C$ ,  $P = 1$  atm - 300 MPa (3kb)
  - Evaporation -  $T = 10 - 40^{\circ}C$ ,  $P = 1$ atm
  - Weathering -  $T = 10 - 100^{\circ}C$ ,  $P = 1$  atm - 10 MPa (0.1 kb)
  - Biological activity -  $T = 10 - 40^{\circ}C$ ,  $P = 1$ atm - 1Mpa.(0.01kb)
- Sublimation from a vapor. This process is somewhat more rare, but can take place at a volcanic vent, or deep in space where the pressure is near vacuum.  $T = 0 - 500^{\circ}C$ ,  $P = 0 - 1$  atm.
- Crystallization from a liquid. This takes place during crystallization of molten rock (magma) either below or at the Earth's surface. Results in igneous rocks,  $T = 600 - 1300^{\circ}C$ ,  $P = 1$ atm - 3,000 MPa (30kb).
- Solid - Solid reactions. This process involves minerals reacting with other minerals in the solid state to produce one or more new minerals.
  - Diagenesis -  $T = 100 - 200^{\circ}C$ ,  $P = 1$  atm - 300 MPa
  - Metamorphism -  $T = 200^{\circ}C$  - melting  $T$ ,  $P = 300 - 1000$  MPa

Thus, for any given system we can define temperature, pressure, and compositional variables that determine what minerals are stable. An understanding of mineral stability is essential in understanding which minerals form, and allow us to determine the conditions present when we encounter minerals in the Earth.

Both temperature and pressure vary with depth in the Earth. Pressure is related to depth because pressure is caused by the weight of the overlying rocks. The way that pressure and temperature vary in the Earth is called the **Geothermal Gradient**.

The average, or sometimes called normal, geothermal gradient in the upper part of the Earth is about  $25^{\circ}C/km$ . But, the geothermal gradient can vary from  $200^{\circ}C/km$  in areas where hot

igneous bodies are intruding at shallow levels of the crust to  $10^{\circ}\text{C}/\text{km}$ , in areas like subduction zones where cold lithosphere descends back into the mantle.



## Phase Diagrams

A phase diagram is a graphical representation of chemical equilibrium. Since chemical equilibrium is dependent on the composition of the system, the pressure, and the temperature, a phase diagram should be able to tell us what phases are in equilibrium for any composition at any temperature and pressure of the system. First, a few terms will be defined.

**System** - A system is that part of the universe which is under consideration. Thus, it may or may not have fixed boundaries, depending on the system. For example, if we are experimenting with a beaker containing salt and water, and all we are interested in is the salt and water contained in that beaker, then our system consists only of salt and water contained in the beaker.

If the system *cannot exchange mass or energy* with its surroundings, then it is termed an **isolated system**. (Our salt and water system, if we put a lid on it to prevent evaporation, and enclosed it in a perfect thermal insulator to prevent it from heating or cooling, would be an isolated system).

If the system *can exchange energy, but not mass* with its surroundings, we call it a **closed system**. (Our beaker, still sealed, but without the thermal insulator is a closed system).

If the system can exchange both mass and energy with its surroundings, we call it an **open system**. (Our beaker - salt - water system open to the air and not insulated is thus an open system).

**Phase** - A phase is a physically separable part of the system with distinct physical and chemical properties. A system must consist of one or more phases. For example, in our salt-water system,

if all of the salt is dissolved in the water, consists of only one phase (a sodium chloride - water solution). If we have too much salt, so that it cannot all dissolve in the water, we have 2 phases, the sodium chloride - water solution and the salt crystals. If we heat our system under sealed conditions, we might have 3 phases, a gas phase consisting mostly of water vapor, the salt crystals, and the sodium chloride - water solution. In a magma, a few kilometers deep in the earth, we might expect one or more phases. For example if it is very hot so that no crystals are present, and there is no free vapor phase, the magma consists of one phase, the liquid. At lower temperature it might contain a vapor phase, a liquid phase, and one or more solid phases. For example, if it contains crystals of plagioclase and olivine, these two minerals would be considered as two separate solid phases because olivine is physically and chemically distinct from plagioclase.

**Component** - Each phase in the system may be considered to be composed of one or more components. The number of components in the system must be the minimum required to define all of the phases. For example, in our system salt and water, we might have the components Na, Cl, H, and O (four components), NaCl, H, and O (three components), NaCl and HO (two components), or NaCl-H<sub>2</sub>O (one component).

### The phase rule

The phase rule is an expression of the number of variables and equations that can be used to describe a system in equilibrium. In simple terms, the *number of variables* are the number of chemical components in the system plus the extensive variables, temperature and pressure. The number of phases present will depend on the variance or *degrees of freedom* of the system. The general form of the phase rule is stated as follows:

$$F = C + 2 - P$$

where F is the number of degrees of freedom or variance of the system.

C is the number of components, as defined above, in the system.

P is the number of phases in equilibrium,

and the 2 comes from the two extensive variables, Pressure and Temperature.

To see how the phase rule works, let's start with a simple one component system - the system Al<sub>2</sub>SiO<sub>5</sub>, shown in the Pressure, Temperature phase diagram below.

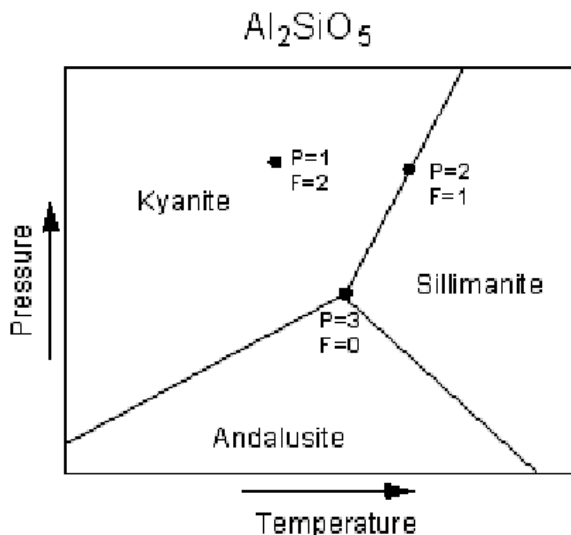
First look at the point in the field of kyanite stability. Since kyanite is the only phase present,  $P=1$ .  $F$  is 2 at this point, because one could change both temperature and pressure by small amounts *without affecting the number of phases present*. We say that this area of kyanite stability on the phase diagram is a divariant field (variance,  $F=2$ ).

Next, look at the point on the phase boundary between kyanite and sillimanite. For any point on such a boundary the number of phases,  $P$ , will be 2. Using the phase rule we find that  $F = 1$ , or there is one degree of freedom. This means there is only one independent variable.

If we change pressure, temperature must also change in order to keep both phases stable. The phase assemblage is said to be univariant in this case, and the phase boundaries are univariant lines (or curves in the more general case).

Finally, we look at the point where all three univariant lines intersect. At this point, 3 phases, kyanite, andalusite, and sillimanite all coexist at equilibrium. Note that this is the only point where all three phases can coexist. For this case,  $P=3$ , and  $F$ , from the phase rule, is 0. There are no degrees of freedom, meaning that any change in pressure or temperature will result in a change in the number of phases. The three phase assemblage in a one component system is said to be invariant.

[N.B.: **Degree of freedom** means the number of extensive variables which you can change without affecting the existing phase or mineral stability. As for example, If two variables of a given system can be changed without affecting mineral stability, degree of freedom of that system is said to be divariant ( $F = 2$ ). If one variable can be changed, then  $F = 1$  (univariant) and if no variables can be changed for keeping the phase or phases stable then the system is said to be invariant ( $F = 0$ )].



## Two Component (Binary) Phase Diagrams

### Experimental determination of two component phase diagrams

As an example, we're going to look at how one might go about determining the stability of a mixture of 2 mineral phases, A and B. To perform these experiments we start with pure minerals A and B and then make mixtures in varying proportions. Each one of these mixtures, plus the pure A and pure B represent different compositions. In this case, we are only going to look at how the stability varies as with temperature and composition, holding Pressure constant at 1 atmosphere.

This type of experiment can be done in a furnace with controlled temperature. Pressure does not have to be controlled because the phase relations will be determined at atmospheric pressure. The various compositions are placed in a capsule that will not react with any of the phases produced. Usually this would be Platinum. Each mixture is then placed in the furnace; the temperature is raised to some point and held at that temperature long enough for equilibrium between all of the phases to occur. The capsules are then quickly removed from the furnace and quenched rapidly. The rapid decrease in temperature that occurs during quenching helps to assure that no further reactions take place and the phase assemblage that was present at the higher temperature is preserved at room temperature. During quenching, any liquid that may have been present at high temperature is found to be glass.

After quenching, each capsule is opened and the phases present are determined using a microscope. In the example shown, we use different symbols to represent the mineral phase assemblages present for each composition run. In this set of experiments 6 different assemblages are found, and are plotted on a

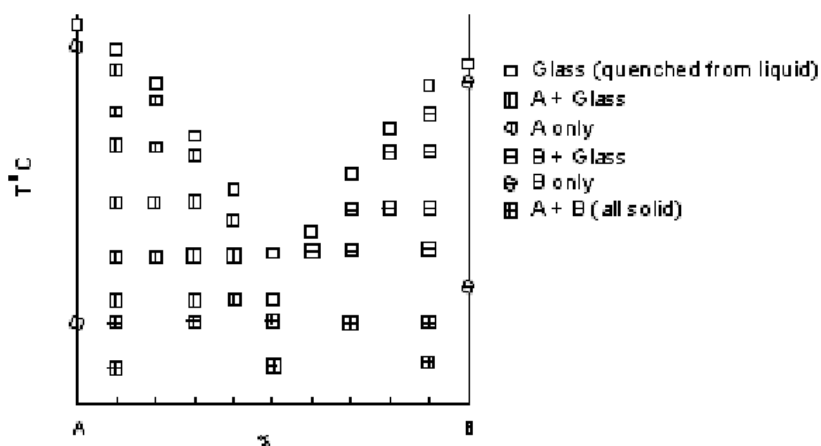
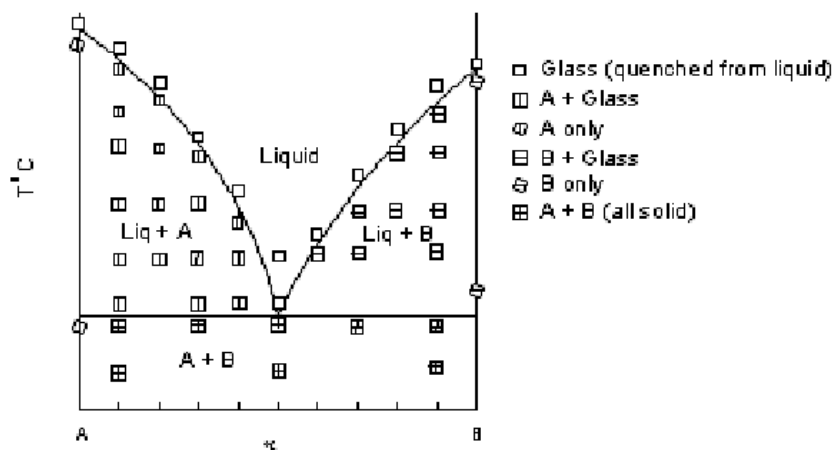


diagram with Temperature of the experiment plotted on the vertical axis, and composition in terms of %A or %B plotted on the horizontal axis.

Note that pure A plots at 100% A which corresponds to 0% B, and pure B plots at 100%B, which corresponds to 0% A.

Note also that no experiments were run at temperatures higher than those where the first complete liquid appeared for each composition.

Once the points are plotted, we can then draw best-fit curves or lines between the data points to determine the Temperature - Composition stability fields for the various phase assemblages. These curves/lines are shown here, and the stability fields for each phase assemblage are labeled. the resulting phase diagram is called a binary eutectic diagram. Not all binary melting diagrams look like this, but this is the simplest and the type that we will discuss first.



## Two component eutectic systems

Figure 1 shows the simplest of two component phase diagrams. The components are A and B, and the possible phases are pure crystals of A, pure crystals of B, and liquid with compositions ranging between pure A and pure B. Compositions are plotted across the bottom of the diagram. Note that composition can be expressed as either a percentage of A or a percentage of B, since the total percentage must add up to 100. (Compositions might also be expressed as mole fraction of A or B, in which case the total must add up to 1). Temperature or pressure is plotted on the vertical axis. For the case shown, we consider pressure to be constant, and therefore have plotted temperature on the vertical axis.

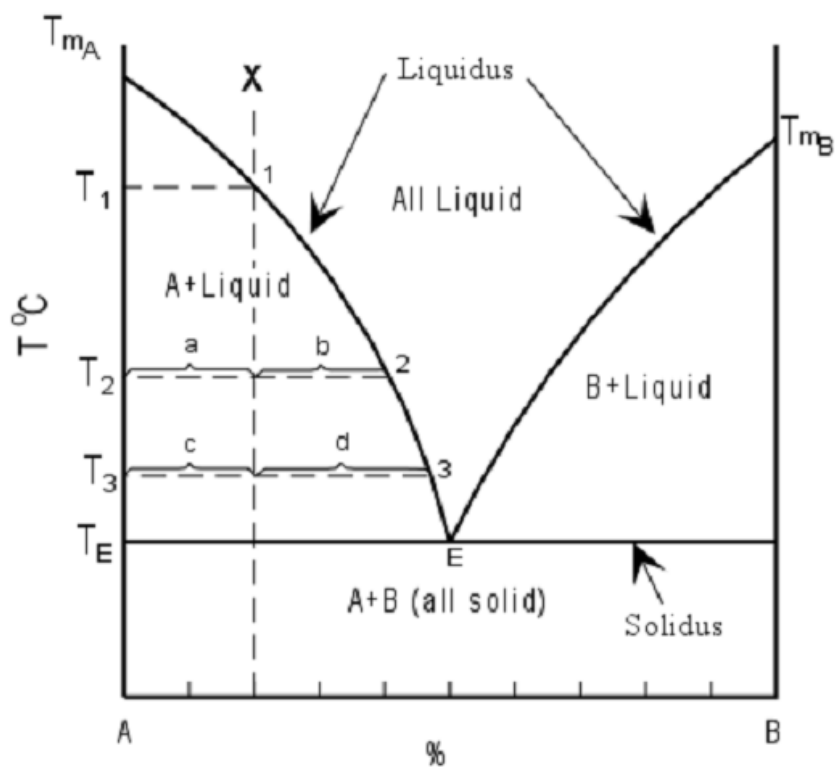


Figure 1



The curves separating the fields of A + Liquid from Liquid and B + Liquid from Liquid are termed **liquidus curves**. The horizontal line separating the fields of A + Liquid and B + Liquid from

Figure 1

A + B all solid, is termed the **solidus**. The point, E, where the liquidus curves and solidus intersect, is termed the **eutectic** point. At the eutectic point in this two component system, all three phases, that is Liquid, crystals of A and crystals of B, all exist in equilibrium. Note that the eutectic is the only point on the diagram where this is true.

Since we looking at a system at constant pressure, the phase rule in this case is  $F = C + 1 - P$ . The eutectic point is therefore an invariant point. If we change the composition of the liquid or the temperature, the number of phases will be reduced to 2.

If the system contains only pure A, then the system is a one component system and phase A melts at only one temperature, the melting temperature of pure A,  $T_{mA}$ . If the system contains only pure B, then it is a one component system and B melts only at the melting temperature of pure B,  $T_{mB}$ .

For all compositions between pure A and pure B, the melting temperature is drastically reduced, and melting begins at the eutectic temperature  $T_E$ . Note that for all compositions between A and B the melting also occurs over a range of temperatures between the solidus and the liquidus. This is true for all compositions except one, that of the eutectic. The eutectic composition melts at only one temperature,  $T_E$ .

We will now consider the crystallization of a liquid with composition X in Figure 1. First, however, we must state the following rule, which must always be obeyed:

**Rule 1 - In equilibrium crystallization or melting in a closed system, the final composition of the system will be identical to the initial composition of the system.**

Therefore, according to rule 1, composition X, which is made up of a mixture of 80% A and 20% B, will have, as its final crystalline product a mixture of 80% crystals of A and 20% crystals of B.

Composition X will be all liquid above the temperature  $T_1$ , because it will lie in the field of all Liquid. If the temperature is lowered to  $T_1$ , at  $T_1$  crystals of A begin to form.

Further lowering of the temperature causes more crystals of A to form. As a result, the liquid composition must become more enriched in B as more crystals of A form out of the liquid. Thus, with lowering of temperature, the liquid composition will change from point 1 to point 2 to point 3 to point E as the temperature is lowered from  $T_1$  to  $T_2$  to  $T_3$  to  $T_E$  respectively. At all temperatures between  $T_1$  and  $T_E$ , two phases will be present in the system; liquid and crystals of A. At the eutectic temperature,  $T_E$ , crystals of B will begin to form, and three phases will

coexist; crystals of A, crystals of B, and liquid. The temperature must remain at  $T_E$  until one of the phases disappears. Thus when the liquid crystallizes completely, only pure solid A and pure solid B will remain and mixture of these two solid phases will be in the proportions of the original mixture, that is 80% A and 20% B.

The crystallization history of composition X can be written in abbreviated form as follows:

$T > T_1$  -- all liquid

$T_1 - T_E$  -- liquid + A

at  $T_E$  -- liquid + A + B

$T < T_E$  -- A + B all solid

If we were to stop the crystallization process at any point during crystallization and observe how much of each phase is present we can use the following example to determine what we would see.

For example, at a temperature  $T_2$  the amount of crystals of A and liquid (the only two phases present at this temperature) could be determined by measuring the distances a and b on figure 1. The percentages would then be given by the lever rule:

$$\% \text{ crystals of A} = b/(a + b) \times 100$$

$$\% \text{ liquid} = a/(a + b) \times 100$$

Note that since the amount of crystals must increase with falling temperature the proportional distance between the vertical line which marks the initial composition and the liquidus increases as temperature falls. Thus the distance used to calculate the amount of solid is always measured toward the liquid side of the initial composition.

At the temperature  $T_3$ , note that more crystals must have formed since the proportional distance  $d/(c+d)$  is greater than the proportional distance  $b/(a+b)$ . Thus at  $T_3$  the lever rule gives:

$$\% \text{ crystals of A} = d/(d + c) \times 100$$

$$\% \text{ liquid} = c/(c + d) \times 100$$

At  $T_3$ , note that the composition of the liquid is given at point 3, i.e. 53% A, the composition of the solid is pure A, and the composition of the system is still 80% A and 20% B. Make sure you understand the difference between composition of the phases and the amount or

percentages of the phases.

The melting process is exactly the reverse of the crystallization process. That is if we started with composition X at some temperature below  $T_E$  the first liquid would form at  $T_E$ . The temperature would remain constant at  $T_E$  until all of the crystals of B were melted. The liquid composition would then change along the liquidus curve from E to point 1 as temperature increased until the temperature  $T_1$  was reached. Above  $T_1$  the system would contain only liquid with a composition of 80% A and 20% B. The melting process in abbreviated form is listed below:

$T < T_E$  -- all solid A + B

at  $T_E$  -- Liquid + A + B

$T_E - T_1$  -- Liquid + A

$T > T_1$  -- all Liquid

## Incongruent melting

*Definition of terms:*

**Liquidus** - The line separating the field of all liquid from that of liquid plus crystals.

**Solidus** - The line separating the field of all solid from that of liquid plus crystals.

**Eutectic point** - The point on a phase diagram where the maximum number of allowable phases are in equilibrium. When this point is reached, the temperature must remain constant until one of the phases disappears. A eutectic is an invariant point.

**Peritectic point** - The point on a phase diagram where a reaction takes place between a previously precipitated phase and the liquid to produce a new solid phase. When this point is reached, the temperature must remain constant until the reaction has run to completion. A peritectic is also an invariant point.

**Intermediate compound** - A phase that has a composition intermediate between two other phases.

**Congruent melting** - melting wherein a phase melts to a liquid with the same composition as the solid.

**Incongruent melting** - melting wherein a phase melts to a liquid with a composition different from the solid and produces a solid of different composition to the original solid.

For the case of incongruent melting, we will use the system forsterite ( $\text{Mg}_2\text{SiO}_4$ ) - silica ( $\text{SiO}_2$ ), which has an intermediate compound, enstatite ( $\text{MgSiO}_3$ ).

This system is a prime example of the phenomena of incongruent melting in rocks, and therefore gives insights into many aspects of mineral formation.

A simplified version of the system forsterite - silica with its intermediate compound enstatite is shown in Figure 2. The crystallization histories for compositions X, Y, and Z will be documented in the following discussion. Each of these compositions behaves in a slightly different manner.

### Crystallization of Composition X

Composition X is a mixture of 13 wt. %  $\text{SiO}_2$  and 87 wt. %  $\text{Mg}_2\text{SiO}_4$ . Because this composition falls between the compositions of pure forsterite and pure enstatite, it must end its crystallization history containing only crystals of forsterite and enstatite. i.e. no quartz will occur in the final crystalline mixture.

If a mixture such as composition X is taken to a temperature above its liquidus (i.e. above  $1800^\circ\text{C}$  in Figure 2) it will be in an all liquid state. We now trace the cooling history of composition X.

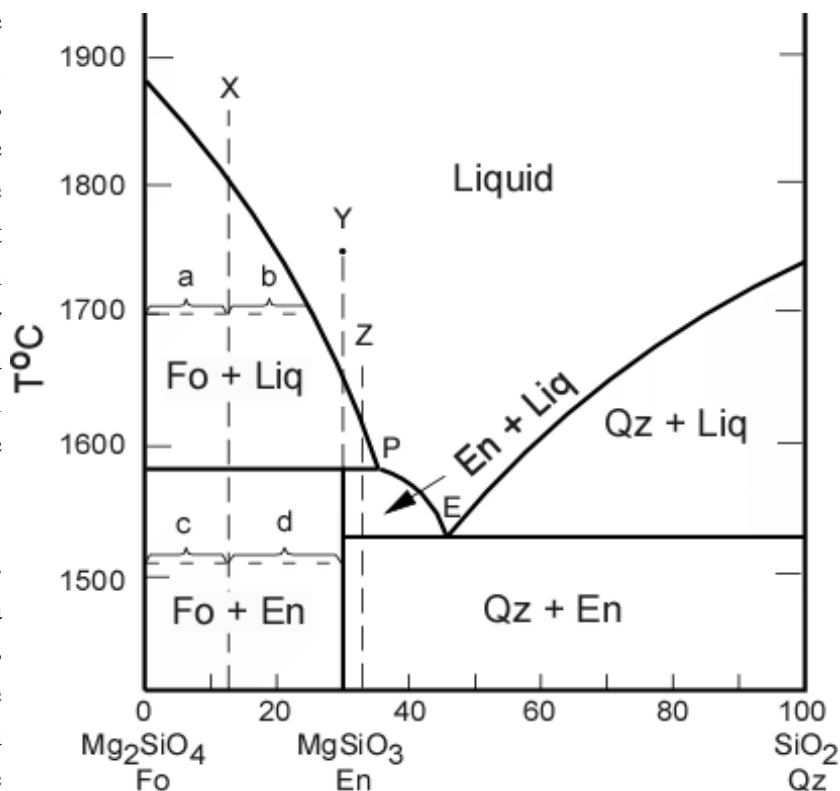
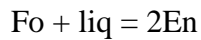


Figure 2

As a liquid of composition X is cooled, nothing will happen until the temperature is equal to the liquidus temperature, 1800°C. At this point crystals of forsterite (Fo) begin to precipitate out of the liquid. As the temperature is further lowered, the composition of the liquid will change along the liquidus toward the peritectic (P), and the crystals forming from the liquid will always be pure Fo until P is reached.

At the temperature of the peritectic, about 1580°, note that three phases must be in equilibrium, Fo, liquid, and enstatite (En). At this point some of the crystals of Fo react with the liquid to produce crystals of En. The reaction that takes place can be written as follows:



(Where SiO<sub>2</sub> in the reaction refers to the component of SiO<sub>2</sub> in liquid with composition P).

After all of the liquid is consumed by this reaction, only crystals of Fo and En will remain. The proportions of Fo and En in the final crystalline product can be found by applying the lever rule.

$$\% \text{Fo crystals} = [d/(c + d)] \times 100$$

$$\% \text{En crystals} = [c/(c + d)] \times 100$$

At any intermediate stage in the process, such as at 1700° the proportion of all phases present (Fo and liquid in this case) can similarly be found by applying the lever rule.

at 1700°C

$$\% \text{Fo crystals} = [b/(a + b)] \times 100$$

$$\% \text{liquid} = [a/(a + b)] \times 100$$

Note that melting of composition X is exactly the reverse of crystallization. Mixture X will begin to melt at the peritectic temperature. At this point En will melt to crystals of Fo plus liquid (incongruent melting). As soon as all of the En crystals have been consumed by this reaction, the temperature can be increased until it reaches 1800° at which point all of the Fo crystals will have been consumed and the only phase left will be liquid with a composition of the starting material.

### Crystallization of Composition Y

Composition Y is equivalent to pure En. Thus only En may appear in the final crystalline product if perfect equilibrium is maintained.

If composition Y is cooled from an all liquid state it first begins to crystallize at about 1650°. At 1650° crystals of Fo will begin to precipitate from the liquid. This will continue with further cooling until the temperature of the peritectic is reached. In this interval, the composition of the

liquid must become more enriched in  $\text{SiO}_2$  and will thus change along the liquidus until it has the composition of the peritectic, P. At the peritectic temperature ( $1580^\circ$ ) all of the remaining liquid will react with all of the previously precipitated Fo to produce crystals of En. The temperature will remain constant until this reaction has gone to completion, after which the only phase present will be pure En.

Thus, it can be seen that enstatite melts incongruently. If pure enstatite is heated to a temperature of  $1580^\circ$  it melts to Fo plus liquid.

### **Crystallization of Composition Z**

Since composition Z lies between En and  $\text{SiO}_2$ , it must end up with crystals of En and Qz (Quartz). If such a composition were cooled from some high temperature where it is in the all liquid state, it would remain all liquid until it reached the liquidus temperature at about  $1600^\circ$ . At this temperature crystals of Fo would begin to precipitate and the composition of the liquid would begin to change along the liquidus toward the peritectic, P. At P, all of the Fo previously precipitated would react with the liquid to produce crystals of En. After this reaction has run to completion, and all of the previously precipitated Fo is consumed, there would still remain some liquid. With decreasing temperature, more crystals of En would form, and the liquid composition would change along the liquidus toward the eutectic, E. At E crystals of Qz would begin to form, the temperature would remain constant until all of the liquid was used up, leaving crystals of Qz and En as the final solid. Note that because composition Z lies very close to the composition of pure En, the final crystalline product would consist mostly of En with a very small amount of Qz.

For all compositions between P and 100%  $\text{SiO}_2$  the system would behave in an identical fashion to the simple Eutectic system discussed previously.

### **Fractional Crystallization in the System**

Up to this point we have always been discussing the case of equilibrium crystallization. That is all solids remain in contact with the liquid until any reaction that takes place has run to completion. As is often the case in natural systems crystals can somehow become separated from the system so that they will not react at reaction points such as P. This is the case of fractional crystallization. Under fractional crystallization conditions the cooling and crystallization histories will be drastically different. In particular, the rule that the final composition must equal the initial composition will not be followed.

As an example of this phenomena we will examine the fractional crystallization of composition X. Furthermore, we will look at the case of perfect fractional crystallization. During perfect fractional crystallization of composition X all of the Fo that is precipitated will be somehow removed from the system. (In nature this can occur by crystals sinking to the bottom of the

liquid due to the fact that crystals generally tend to be more dense than liquids.) Note that if only some of the crystals are removed from the liquid we will have a case intermediate between perfect fractional crystallization and equilibrium crystallization.

Cooling a liquid of composition X to the liquidus at  $1800^{\circ}$  will cause Fo to precipitate as before. With further cooling the liquid composition will change along the liquidus and more Fo will be precipitated. In this case, however, all of the Fo will be removed from the system as it crystallizes. Since the Fo is no longer present, the composition of the system will have the composition of the liquid (the Fo removed can no longer contribute to the composition of the system). Therefore, when the temperature reaches the peritectic temperature,  $1580^{\circ}$ , there will be no Fo available to react with the liquid, and the liquid (and system) will have a composition, P. Thus the liquid will now precipitate crystals of En and continue cooling to the eutectic, E, where crystals of Qz will form. The final crystalline product will consist of Qz and En.

Compare this case with the previously discussed case of equilibrium crystallization of composition X. Note that under equilibrium conditions the final crystalline product of composition X contained crystals of Fo and En, while in the fractional crystallization case the final product contains En and Qz. Thus fractional crystallization has allowed an originally Fo rich composition to produce an  $\text{SiO}_2$  rich liquid and Qz appears in the final crystalline product.

If you go back and look at simple eutectic systems, or look at fractional crystallization of composition Z in the more complex system, you should be able to see that fractional crystallization will have no effect on the phases produced in the final crystalline product, but will only change the proportions of the phases produced. Fractional crystallization is only effective in producing a different final phase assemblage if there is a reaction relationship of one of the phases to the liquid.

## **Solid solution systems**

In the systems we've discussed so far, all of the mineral or solid phases have been pure phases, that is they have one and only one possible composition. This is not usually the case in nature, since substitution of one element for another often occurs due to the fact that some elements behave in a chemically similar fashion to other elements. When such substitutions occur, the phase can have a range of possible compositions, depending on the amount of substitution that takes place. Such solids that can have various amounts of elemental substitution are called solid solutions. A good example of a solid solution mineral is the mineral olivine. The general chemical formula for olivine is  $(\text{Mg,Fe})_2\text{SiO}_4$ . Since  $\text{Mg}^{+2}$  and  $\text{Fe}^{+2}$  are about the same size and have the same charge, they may substitute for one another in the crystal structure of olivine. Thus olivine may have a composition anywhere between the pure Mg end member, forsterite

( $\text{Mg}_2\text{SiO}_4$ ), and the pure Fe end member, fayalite ( $\text{Fe}_2\text{SiO}_4$ ). When all compositions between two end members are possible, the solid solution is said to be a complete solid solution.

Another good example of a complete solid solution is displayed in the plagioclase feldspars. In this case the solid solution is between the end members albite ( $\text{NaAlSi}_3\text{O}_8$ ) and anorthite ( $\text{CaAl}_2\text{Si}_2\text{O}_8$ ). In order to maintain charge balance we cannot simply substitute  $\text{Na}^+$  for  $\text{Ca}^{+2}$ , so this solid solution is what is called a coupled solid solution. In this case  $\text{Na}^+\text{Si}^{+4}$  is substituted for  $\text{Ca}^{+2}\text{Al}^{+3}$  in the plagioclase structure to produce intermediate compositions of plagioclase.

Because the elements that substitute are not exactly the same size (they are similar in size) the amount of substitution is dependent on temperature and pressure and the solid solutions behave in a somewhat orderly fashion as illustrated below.

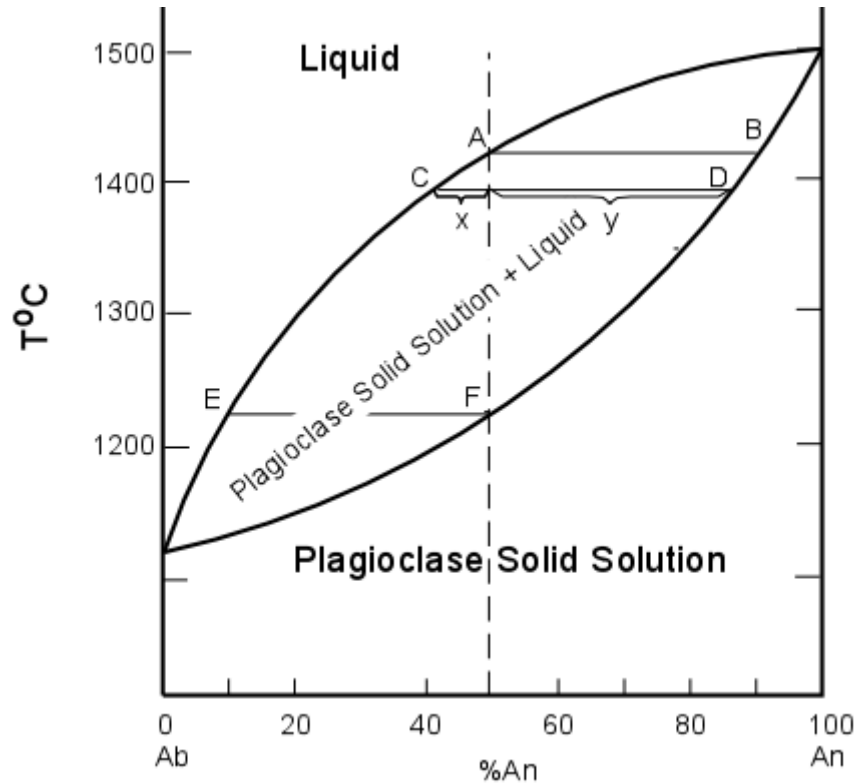
Since plagioclase is one of the most common minerals in the earth's crust, we will discuss the phase diagram for the plagioclase system. The phase relations in the plagioclase system are shown in Figure 3 at constant pressure equal to that of the atmosphere (atmospheric pressure is 1 bar). In Figure 3 the upper curve is called the liquidus and the lower curve is called the solidus. At temperatures above the liquidus everything is liquid, below the solidus everything is solid (crystals of plagioclase solid solution). At temperatures between the solidus and liquidus crystals of plagioclase solid solution coexist in equilibrium with liquid.

Pure albite melts (or crystallizes) at  $1118^\circ\text{C}$ , and pure anorthite melts (or crystallizes) at  $1500^\circ\text{C}$ . Note that any composition of plagioclase between the two end members melts or crystallizes over a range of temperatures unlike the pure end members which have only one melting point. Thus we can read from the diagram that a solid solution containing 50% albite and 50% anorthite ( $\text{Ab}_{50}\text{An}_{50}$ ) begins to melt at  $1220^\circ$ , point F, and the melting is complete at  $1410^\circ$ , point A. Inversely, if a melt of composition  $\text{Ab}_{50}\text{An}_{50}$  is cooled it will begin to crystallize at  $1410^\circ$  and will be completely crystalline at  $1220^\circ$ .

We will now trace the crystallization history of composition X, which is  $\text{Ab}_{50}\text{An}_{50}$ . Composition X is completely liquid above the liquidus (above  $1410^\circ$ ). Cooling to the liquidus at point A results in the crystallization of a small amount of plagioclase solid solution. The composition of this plagioclase can be found by drawing an isotherm (line of constant temperature, a horizontal line in this diagram) through the temperature  $1410^\circ$ . Where this isotherm intersects the solidus (at point B), the composition of the solid can be found by drawing a vertical line to the base of the diagram. Thus it is seen that the first crystals precipitated from composition X will have the composition  $\text{Ab}_{10}\text{An}_{90}$ . Note that in this diagram crystals that are in equilibrium with liquid will always be enriched in anorthite component relative to the liquid. As crystallization continues with lowering of temperature the composition of the plagioclase will change along the solidus, continually reacting with the liquid to produce crystals more enriched in the Ab component. Meanwhile, the composition of the liquid will change along the liquidus, thus also becoming more enriched in the Ab component. At a temperature of  $1395^\circ$  the liquid composition will be at



point C, while the solid composition will be at point D. Crystallization proceeds until a temperature of about 1220°, at which point the last remaining liquid will have a composition at E, and the solid will have a composition equal to the original starting composition at point F. At this point all of the liquid will be consumed and the final crystalline product will have the composition Ab<sub>50</sub>An<sub>50</sub>.



**Figure 3**

During crystallization the proportion of the solid continually increases while that of the liquid continually decreases. Thus as the composition of the liquid becomes more sodic, approaching E, its volume steadily decreases. Thus it can be seen that the amount of liquid in equilibrium with the solid of composition F will be extremely small.

If at any point during the crystallization we wish to determine the amount of solid and liquid, we can apply the lever rule. As an example, we will determine the proportions of liquid and solid in the system at a temperature of 1395°. At this point, we measure the distances oC, oD, and CD. The percentages of liquid and solid are then given as follows:

$$\% \text{ solid (with composition D)} = [x/(x + y)] \times 100$$

$$\% \text{ liquid (with composition C)} = [y/(x + y)] \times 100$$

The foregoing discussion assumes that equilibrium is maintained throughout the course of crystallization. This means that with falling temperature and continuing crystallization, the earlier-formed, more calcic crystals must react continuously with the liquid to produce homogeneous crystals that will become continuously more enriched in the sodic component. If this equilibrium cannot be maintained, then fractional crystallization will take place.

We will distinguish between three contrasting conditions.

1. In equilibrium crystallization, the crystals remain suspended in the melt, and cooling and crystallization are slow enough to allow continuous, complete reaction between crystals and melt. The early formed crystals will, on cooling, react with the melt continuously and thereby gradually change their composition along the solidus from B to F, while simultaneously the liquid changes from A to E. In such circumstances the crystals will not change composition beyond F, and the end product is a homogeneous mixed crystal (solid solution) having the same composition as the initial melt.
2. Assume that the crystals are continuously removed from the melt, by sinking or some natural filtering process. Reaction of crystals with the melt is prevented, and the composition of the liquid will continue to change along the liquidus curve toward the sodic feldspar component. The only limit to this change of composition of the liquid is the composition of the pure Na feldspar, but the relative amount of very sodic liquid would be very small. As the liquid phase changed composition with continuing removal of crystals, the successively formed crystals would become continuously more sodic; the final product would be pure albite, but it would constitute a very small proportion of the initial amount.
3. If the crystals remain suspended in the liquid, but relatively rapid crystallization does not allow complete reaction between crystals and liquid, the effect will be somewhat different. In effect, failure to react completely partially removes the already formed crystals from the system. The melt becomes increasingly more sodic, and earlier formed more calcic crystals serve as nuclei on which increasingly more sodic feldspar crystallizes. The resulting crystal contain zones of differing composition; the inner zones being more calcic, and the outer zones more sodic. The bulk (average) composition of the zoned crystal is that of the initial system, but the range of composition between the inner and outer zones might theoretically be as large as from B to pure Ab in the example shown for composition X.

## **Exsolution**

Many minerals that show complete solid solution at higher temperatures do not show such solid solution at lower temperatures. When this is the case, the phenomenon of exsolution occurs. Since solid solutions are really one mineral phase dissolved in another mineral phase to form a

single mineral phase, exsolution implies that one or the other of the mineral phases in the solution must "exsolve" or come out of solution with the other mineral phase.

Figure 3 illustrates a phase diagram (much simplified) of the alkali feldspar system which exhibits such exsolution behavior at low temperatures. At high temperatures the diagram shows that albite (Ab) or  $\text{NaAlSi}_3\text{O}_8$  and orthoclase (Or) or  $\text{KAlSi}_3\text{O}_8$  form a complete solid solution series. This solid solution series is different from the plagioclase solid solution series only in that it has a minimum composition in the middle rather than at the composition of one of the pure end members. At temperatures just below the solidus, alkali feldspar solid solutions are stable. At lower temperatures, along the curve labeled "solvus" the solid solution is no longer stable.

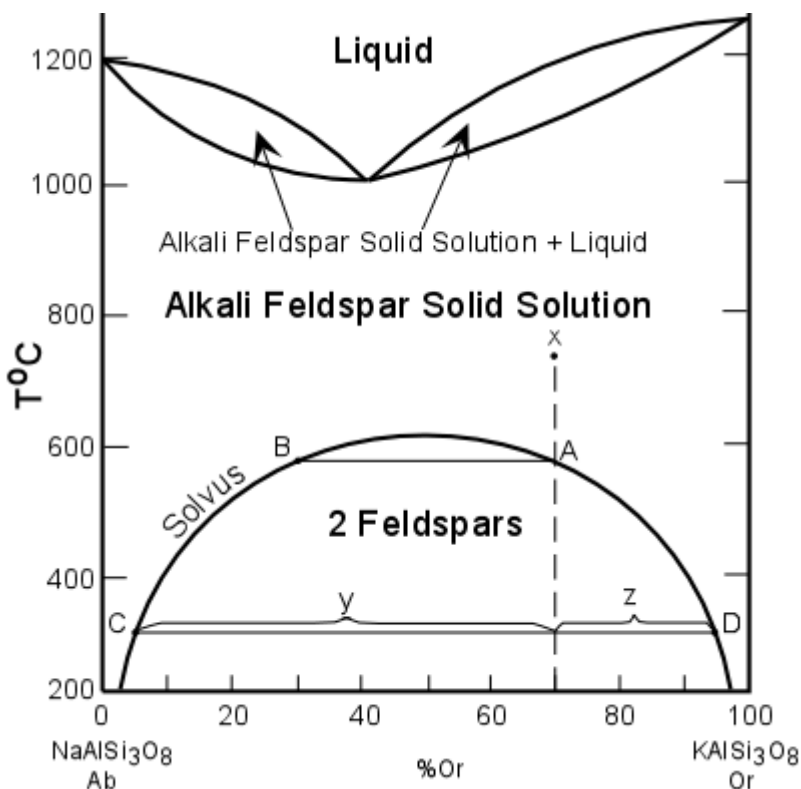


Figure 4

This solid solution remains stable with lowering of temperature until the temperature of the solvus is obtained at point A (a temperature of about  $590^\circ$ ). At this temperature the solid solution is no longer stable and begins to exsolve. The composition of coexisting exsolved phases can be found by drawing an isotherm until it intersects the solvus. Such an isotherm at  $590^\circ$  shows that at this temperature a solid solution having the composition of point B ( $\text{Or}_{32}\text{Ab}_{68}$ ) coexists with an alkali feldspar solid solution with the composition of point A ( $\text{Or}_{70}\text{Ab}_{30}$ ). With further lowering of temperature further exsolution occurs. At a temperature of  $300^\circ$  our original composition X has exsolved into two alkali feldspar solid solutions, one with the composition of point C and one with a composition of point D. To find the relative

In this case the exsolution phenomena occurs below the solidus and so is a "*sub-solidus*" reaction. In order to see what happens during exsolution we will examine what happens to a composition labeled X in Figure 4. We will start at a temperature of 750° in the region where alkali feldspar solid solutions are stable. At 750° the composition of the alkali feldspar solid solution is 70% orthoclase and 30% albite (Or<sub>70</sub>Ab<sub>30</sub>).

proportions or percentages of each of the solid solutions, the lever rule can once again be applied. For example at 300° for composition X the percentage of the albite-rich solid solution is  $[z/(z+y)] \times 100$ , while that of the orthoclase-rich solid solution is  $[y/(z+y)] \times 100$ . With further lowering of temperature all of the albite and orthoclase in the two solid solutions could exsolve completely to produce a pure albite phase and a pure orthoclase phase. Such complete exsolution does occur in nature, but only if the temperature is lowered very slowly. Complete exsolution is only common in metamorphic rocks. More often, especially in granitic rocks, the two exsolved phases do not separate as individual crystals, but occur as intergrown crystals with exsolution lamellae of one crystal occurring within the other crystal. In the alkali feldspars containing such exsolution lamellae the result is to produce a texture called perthitic or perthite. Perthite on a microscopic scale is illustrated on page 540, figure 19.77 of your mineralogy text (Klein and Dutrow).

### Examples of Questions on this material that could be asked on an exam

1. First note that phase diagrams similar to any of the above could be presented on an exam and you could be asked to (a) trace the crystallization history of any specified composition, (b) determine the temperatures of first melting of any specified composition, (c) determine the composition of all phases present in any specified composition at a specified temperature and pressure, and (c) determine the proportions of all phases present in a specified composition at a specified temperature.
2. Define the following: (a) liquidus, (b) solidus, (c) solvus, (d) fractional crystallization (e) solid solution, (f) incongruently melting compound.
3. Draw examples of phase diagrams that show the following - be sure to label everything.
  - a. a phase diagram that has an intermediate compound that melts incongruently.
  - b. a phase diagram that shows complete solid solution between two end members.
  - c. a phase diagram that shows complete solid solution at high temperature and exsolution at low temperature.